



THE MOMBASA POLYTECHNIC UNIVERSITY COLLEGE

(A Constituent College of JKUAT)

Faculty of Engineering and Technology

DEPARTMENT OF ELECTRICAL & ELECTRONIC ENGINEERING

**UNIVERSITY EXAMINATION FOR DEGREE IN BACHELOR OF
SCIENCE/ENGINEERING IN ELECTRICAL & ELECTRONIC
ENGINEERING
YR 3, SEM 1**

EEE 4303: ELECTROMAGNETIC WAVES
EEE 2304: ELECTROMAGNETICS II

**END OF SEMESTER EXAMINATION
SERIES: DECEMBER 2011
TIME: 2 HOURS**

Instructions to Candidates:

This paper consists of **FIVE** questions

- *Answer Booklet*

Answer question **ONE (COMPULSORY)** and any other **TWO** questions

Marks are indicated for each part of the question

This paper consists of **FOUR** printed pages

Question One

- a) Write down Maxwell's equations in integral form and explain the significance of each in electromagnetic theory (4 marks)

$$\vec{E} = 20 \cos(\omega t - 50x) \hat{a}_y \text{ v/m}$$

- b) In free space (10 marks)

Determine:

- (i) I_d
- (ii) \vec{w}
- (iii) \vec{H}

- c) Suppose that a uniform plane wave is travelling in the x direction in a lossless dielectric ($\epsilon_r = 1$) with the 100V/m electric field component in the $-z$ direction. If the wavelength is 25cm and the velocity of propagation is $2 \times 10^8 \text{ ms}^{-1}$. Draw the phasor diagram of the electric and magnetic field vectors and determine the:

- (i) Frequency of the wave
- (ii) Relative permittivity of the medium
- (iii) Complete time domain expressions for the electric and magnetic field expressions
- (iv) Average power density (11 marks)

- d) An electric EM wave travelling in medium 1 is incident on a material boundary with medium 2 as shown in figure Q1 (d). Determine the general phasor expressions for the electric and magnetic fields for the:

- (i) Incident wave
- (ii) Reflected wave
- (iii) Transmitted wave (5 marks)

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Question Two

- a) Determine using the phasor method, whether the following field vectors satisfy both Farady's and Ampere's laws in free space.

$$\hat{E}_x = 20\pi e^{-\alpha y} \cos(\omega t - \beta z) \quad \text{V/m} \quad \hat{a}_x$$

$$\hat{B} = \mu_0 H_m e^{-\alpha y} \cos(\omega t - \beta z) \quad \hat{a}_y$$

(14 marks)

- b) Write down the phasor and time domain expressions for a 5MHz uniform plane wave travelling in free space. The 10V electric field intensity vector is directed in the +z direction and the wave is propagating in -y direction (sketch the field vectors) (6 marks)

Question Three

Given Maxwell's equations.

$$\nabla \times \hat{E} = -j\omega \mu_0 \hat{H}$$

$$\nabla \times \hat{H} = j\omega \epsilon_0 \hat{E}$$

$$\hat{E} = E_m^+ e^{-j\beta z} + E_m^- e^{j\beta z}$$

$$\hat{H}_y = H^+ e^{-j\beta z} + H^- e^{j\beta z}$$

Prove that

Explain all your steps and justify any assumptions made

(20 marks)

Question Four

- a) With reference to fig Q4(a), medium 1 is air and medium 2 is Teylon ($\mu_r = 1$). Assume the Teylon is infinitely thick so that no reflected waves exist in the Teylon ($\epsilon_r = 2.1$).

Write the time domain expressions for all the fields in these two media if the transmitted electric

$$E^t = 10 \cos\left(\omega t - \left(\frac{8\pi}{3}\right)z\right) \hat{a}_x$$

field in medium 2 is measured as

(13 marks)

- b) Determine the average incident, reflected and transmitted power density of the plane wave and show that energy is conserved across the interface (7 marks)

Question Five

- a) Explain with the aid of a sketch, why TEM waves cannot exist in a single conductor hollow (or dielectric filled) waveguide (5 marks)
- b) Describe energy modes and show how they relate to the wave guide cut-off frequency
- c) An air-filled rectangular waveguide has cross sectional dimensions:

$$X = 3.0 \text{ cm}$$

$$y = 1.5 \text{ cm}$$

Find the cut off frequency for the following modes:

- (i) TE₁₀
- (ii) TE₂₀
- (iii) TE₀₁
- (iv) TE₀₂

- d) Identify with justifications the degenerate and dominant modes in (c) (15 marks)