# THE MOMBASA POLYTECHNIC UNIVERSITY COLLEGE <br> (A Constituent College of JKUAT) <br> Faculty of Engineering and Technology 

DEPARTMENT OF BUILDING AND CIVIL ENGINEERING
UNIVERSITY EXAMINATION FOR DEGREE IN BACHELOR OF SCIENCE IN CIVIL ENGINEERING

ECE 2317: THEORY OF STRUCTURES IV

## END OF SEMESTER EXAMINATION

SERIES: DECEMBER 2011
TIME: 2 HOURS

## Instructions to Candidates:

You should have the following for this examination

- Answer booklet
- Battery Powered Programmable Calculators may be used

This paper consists of FIVE questions
Answer question ONE (COMPULSORY) from SECTION A and any other TWO questions from SECTION B
Maximum marks for each part of a question are clearly shown
This paper consists of THREE printed pages

## SECTION A (COMPULSORY)

## Question 1 (30 marks)

a) State the following:
(i) Castigliano’s First Theorem
(2 marks)
(ii) Castigliano Second Theorem
(2 marks)
(iii) First Moment of Area Theorem
(2 marks)
(iv) Second Moment of Area Theorem
(2 marks)
(v) Principle of Virtual Work
(2 marks)
b) A beam $A B C$ is simply supported at $A$ and $B$ and overhangs from $B$ to $C$. The span from $A$ to $B$ has a length of 10 m , and the overhand has a length of 4 m . A concentrated load of 40 KN acts at point D , which is 4 m from the support at A , and another concentrated load of 10 KN acts at C on


#### Abstract

$\theta_{A} \quad \theta_{B}$ the overhand. Using the moment area method, calculate the angles of rotation and and the $\delta_{c}$ deflection at the free end C Figure 1 (Take E = 200GPa and $\mathrm{I}=1.28 \mathrm{X} 10^{9} \mathrm{~mm}^{4}$


## SECTION B (Answer any TWO questions from this section)

## Question 2 (20 marks)

Using Castigliano’s First Theorem determine the vertical deflection at node 3 marks)

Figure 2 (Take $E=210 \mathrm{KN} / \mathrm{mm}^{2}$ and $5 \mathrm{~cm}^{2}$ for all members)

## Question 3 (20 marks)

The beam shown is of constant modulus throughout. It is loaded with a single concentrated load of 10 KN at end A of the overhang AB . The beam has an internal pin at C. Using the conjugate beam method
(i) Find the displacement and rotation at point A
(ii) Sketch the deflection diagram and lable the important points

Figure 3 (Take El = $10 \mathrm{MNm}^{2}$ )

## Question 4 (20 marks)

Using Castigliano's Second Theorem determine the member forces in the braced frame shown in the figure below taking 2-5 to be the redundant member

Figure 4 (Assume EA is constant for all members)

## Question 5 (20 marks)

The single-bay portal frame ABCDE shown below is of constant cross-section throughout, and pinned to rigid foundations at A and D. It is loaded along the beam with 10 KN centrally placed and a uniformly distributed load of $15 \mathrm{KN} / \mathrm{m}$.

Determine the bending moment at B and C and draw the bending moment diagram
Figure 5

