# TECHNICAL UNIVERISTY OF MOMBASA Faculty of Engineering \& Technology 

DEPARTMENT OF COMPUTER SCIENCE \& INFORMATION TECHNOLOGY
UNIVERSITY EXAMINATIONS FOR DEGREE IN:
BACHELOR OF TECHNOLOGY IN INFORAMATION TECHNOLOGY (Y1)
EIT 4110: DISCRETE STRUCTURES

## END OF SEMESTER EXAMINATION <br> SERIES: APRIL 2015 <br> TIME: 2 HOURS

## Instructions to Candidates:

You should have the following for this examination

- Answer Booklet

This paper consists of FIVE questions.
Attempt question ONE (Compulsory) and any other TWO questions
Maximum marks for each part of a question are as shown
This paper consists of THREE printed pages

## Question One (Compulsory)

a) State the meanings of het following symbols:
(i)
(ii) $V$
$\phi$
(iii)
marks)
b) Using examples, show the meaning of the following words as used in set theory:
(i) Singleton
(ii) Doubleton
(iii) Tripleton marks)
c) Write the English meaning of the following expression:
$(x \in\{x ; x$ is tal $\} \leftrightarrow x$ is tall $)$
$\forall_{x}$
(6 marks)
d) Use a Venn diagram to represent the relationship

$$
A \cap B
$$

e) Let $U=(1,2,3,4,5) \quad S \subseteq U$ be Let 4,5$\}$ Determine $\mathrm{S}^{\text {c }}$

## Question Two

a) Which of the following are sets? Assume that a proper universal set has been chosen:

$$
A=\{2,3,5,7,11,13,19\}
$$

(i) $B=\{A, E, I, O, U\}$
(ii)

$$
C=\{\sqrt{x}: x<\phi\}
$$

(iii)

$$
D=\{1,2, A, B, Q, 1, V\}
$$

(iv)
(v) E is a list of all people in your phone book
b) Give Venn diagram representation for the following sets:
(i) $\mathrm{A}-\mathrm{B}$
(ii) $\mathrm{B}-\mathrm{A}$

$$
A^{\subset} \cap B
$$

(iii)
$A \Delta B$
(iv)
$(A \Delta B)^{c}$
(v)
(10 marks)

## Question Three

$$
f: N \rightarrow N
$$

a) Suppose is given by:

$$
f(n)=2 n
$$

$$
g: N \rightarrow N
$$

while of is given by:

$$
g(n)=n+4
$$

Determine:

$$
\text { (i) } \begin{aligned}
& (g \circ f)(n) \\
& (f \circ g)(n)
\end{aligned}
$$

(4 marks)
(ii)
b) Determine a, b, c, d in the following truth table

| X | Y | X or Y |
| :--- | :--- | :--- |
| 0 | 0 | a |
| 0 | 1 | b |


| 1 | 0 | C |
| :--- | :--- | :--- |
| 1 | 1 | d |

c) Determine a and b in the following table

| X | Not X |
| :--- | :--- |
| 0 | a |
| 1 | b |

## Question Four

a) Fill in the blanks

| a | b | c | $\mathrm{b}^{*} \mathrm{c}$ | $\mathrm{a}+\left(\mathrm{b}^{*} \mathrm{c}\right)$ | $\mathrm{a}+\mathrm{b}$ | $(\mathrm{a}+\mathrm{b})^{*}$ | $(\mathrm{a}+\mathrm{b})^{*}(\mathrm{a}+\mathrm{c})$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 0 | 0 |  |  |  |  |  |
| 0 | 0 | 1 |  |  |  |  |  |
| 0 | 1 | 0 |  |  |  |  |  |
| 1 | 1 | 1 |  |  |  |  |  |
| 1 | 0 | 0 |  |  |  |  |  |
| 1 | 0 | 1 |  |  |  |  |  |
| 1 | 1 | 0 |  |  |  |  |  |
| 1 | 1 | 1 |  |  |  |  |  |

## Question Five

a) Use the properties of Boolean Algebra to prove that:

$$
(a+b)(a+a)=a
$$

b) Convert the following equation to logic gates:
F = a AND NOT (b OR NOT (c) )

