



TECHNICAL UNIVERSITY OF MOMBASA

**Faculty of Engineering & Technology  
in Conjunction with  
Kenya Institute of Highways and  
Building & Technology (KIHBT)**

DEPARTMENT OF ELECTRICAL & ELECTRONIC ENGINEERING

HIGHER DIPLOMA IN TECHNOLOGY

ECI 3201: CONTROL ENGINEERING

END OF SEMESTER EXAMINATION

SERIES: MAY 2015

TIME ALLOWED: 2 HOURS

**Instructions to Candidates:**

You should have the following for this examination

- *Answer Booklet*

This paper consists of **FIVE** questions. Answer any **THREE** questions  
This paper consists of **FOUR** printed pages

### Question One

a) With the aid of a diagram, define the following terms as used in specifying the transient response characteristics of a control system to a unit step input:

- (i) Delay time,  $t_d$
- (ii) Rise time,  $t_r$
- (iii) peak time,  $t_p$
- (iv) Maximum overshoot,  $M_p$
- (v) Settling time,  $t_s$

**(12 marks)**

b) Consider the system with the transfer function:

$$G(s) = \frac{1}{(s+1)(s+2)}$$

Obtain the gain and phase shift of  $G(s)$  for  $\omega = 2$  and  $\omega = 10$

**(8 marks)**

### Question Two

a) A system is described by the following differential equation:

$$4 \frac{dy}{dt} + 2y = 210^{-3} x$$

Determine:

$$G(s) = y(s) / x(s)$$

- (i) The transfer function
- (ii) Time constant,  $t$  and the steady state gain,  $K$  Expression for
- (iii) Time response to a unit step input

**(12 marks)**

b (i) State the routh stability criterion

(ii) The open loop transfer function of a unity feedback control system is given as:

$$G(s) = \frac{1}{s^3 + 3s^2 + 3s + 1 + k}$$

Using the Routh stability criterion, what restrictions must be placed upon the parameter  $k$  in order to ensure that the system is stable

**(8 marks)**

### Question Three

a) (i) Explain the term compensation as applied to control system.

(ii) An R-C network mechanization of a lead compensator is shown in figure Q3(a). Find its transfer function

**(12 marks)**

b) A closed loop control system with negative feedback has:

$$G(s) = \frac{2}{s(1+s)}$$

$$H(s) = \frac{2}{1+0.5s}$$

- (i) Write down an expression for the open loop transfer function
- (ii) Sketch the Nyquist diagram and comment on the stability of the system

**(8 marks)**

#### Question Four

a) Consider the following second-order differential system given:

$$\frac{d^2y}{dt^2} + 5\frac{dy}{dt} + 9y = 9u$$

Determine:

- (i) The undamped natural frequency  $\omega_n$
- (ii) The damping ratio  $\zeta$
- (iii) The time constant  $\tau$

- (iv) The damped natural frequency  $\omega_\delta$  **(12 marks)**

b) (i) Name any THREE standard test signals that commonly used for system performance analysis.

- (ii) State the justification of using the test signals mentioned in (i) **(8 marks)**

#### Question Five

a) Simplify the block diagram given in figure Q5(a) to a canonical form **(10 marks)**

- b)** Consider a system shown in figure Q5bi when it is subjected to a unit-step input the system output responds as shown in figure Q5b ii.  
Determine the values of  $K$  and  $T$  from the response curve