



THE MOMBASA POLYTECHNIC UNIVERSITY COLLEGE

(A Constituent College of Jkuat)

Faculty of Applied & Health Sciences

DEPARTMENT OF PURE & APPLIED SCIENCE

AMA 2103: CALCULUS FOR SCIENCE

END OF SEMESTER EXAMINATION

SERIES: AUGUST/SEPTEMBER 2011

TIME: 2 HOURS

Instructions to Candidates:

Answer questions **ONE** which is (**COMPULSORY**) and any other **TWO** questions

Calculators may be used

This paper consist of **THREE** printed pages

Question One

a) i) (5 marks)

ii) Given

Find the velocity and acceleration of the projectile at (6 marks)

b) i) Differentiate by first principals

$$y = x^2 + 2x + 1$$

(6 marks)

ii) Differentiate with respect to x

$$y = \ln x \cos x$$

(4 marks)

iii) Determine the turning points of the curve

$$y = 4x^3 - 48x + 2$$

(9 marks)

Question Two

a) Differentiate with respect to x to determine $\frac{dy}{dx}$ and $\frac{d^2y}{dx^2}$ (10 marks)

$$x^2 + y^2 - 2x - 6y + 5, \quad x = 3, y = 2$$

at

b) Given $x = \frac{4-3t}{2+t}, y = \frac{5+2t}{2+t},$ Determine $\frac{dy}{dx}$ (10 marks)

Question Three

a) Find the equation of the tangent and normal to the curve

$$x^3 + y^2y + y^3 - 8 = 0,$$

at (1,0)

(10 marks)

b) (i) Find the length of the curve

$$y^2 = x^3$$

Between $x = 0$ and $x = 4$

(5 marks)

(ii) Find the area bounded by the curve

$$y = x^2 - 9$$

and the x -axis and between $x = -3$ and $x = 3$

(5 marks)

Question Four

$$Z = \frac{2x - y}{x + y}$$

a) If
Find;

$$\frac{\partial z}{\partial x}$$

(i)

(3 marks)

$$\frac{\partial z}{\partial y}$$

(ii)

(3 marks)

$$\int \frac{x+1}{x^2 - 3x + 2} dx$$

b) (i)

(9 marks)

$$\int \sin^3 x dx$$

(ii)

(5 marks)

Question Five

a) Given the data

x	5 - 9	10 - 14	15 - 19	20 - 24	25 - 29	30 - 34
f	4	9	16	12	6	3

Determine;

i) Mean

(4 marks)

ii) Mode

(3 marks)

iii) Median

(3 marks)

iv) Standard Deviation

(3 marks)

b) It has been established that 16% of all glass ware received by a certain organization are defective.

Determine;

- i) The probability that any one item is defective (1 mark)
- ii) The probability that any one item is acceptable (1 mark)
- iii) If at one time 5050 items were received, how many were likely to be acceptable
(2 marks)
- iv) If the cost of an item is Ksh. 425.50, find the likely loss the organization will occur when 5050 items are received. (3 marks) [;/'