



THE MOMBASA POLYTECHNIC UNIVERSITY COLLEGE

(A Constituent College of Jkuat)

Faculty of Engineering and Technology

DEPARTMENT OF BUILDING AND CIVIL ENGINEERING

DIPLOMA IN BUILDING & CIVIL ENGINEERING (DBCE II)
DIPLOMA IN CIVIL ENGINEERING (DCEN II)

AMA 2101: ALGEBRA

END OF SEMESTER EXAMINATION

SERIES: AUGUST/SEPTEMBER 2011

TIME: 2 HOURS

Instructions to Candidates:

You should have the following for this examination

- *Answer booklet*
- *Mathematical table*
- *Pocket calculator*

This paper consists of **FIVE** questions

Answer question **ONE** and any other **TWO** questions

Maximum marks for each part of a question are as shown

This paper consists of **THREE** printed pages
SECTION A (COMPULSORY)

Question 1

a) Use logarithms to evaluate:

$$\frac{3.28 \times (5.86)^2}{\sqrt{0.1486 \times 4.56}}$$

(8 marks)

b) Solve the following equations:

$$\frac{2x-1}{x-1} = \frac{3x-4}{x+4}$$

(i)

$$3(x-1) + (x-1)^2 = 1$$

(ii)

(12 marks)

$$\left(1 - \frac{1}{2}x\right)^6$$

c) Use binomial theorem to expand $\left(1 - \frac{1}{2}x\right)^6$ up to the fifth term. Hence find the value of $(0.96)^6$ correct to three decimal places (10 marks)

SECTION B (Answer any TWO questions from this section)

Question 2

$$y = kb^x$$

a) Two quantities x and y are related by a law of the form $y = kb^x$. Using the values given in the Table 1, verify the law graphically. Hence find the approximate values of the constants k and b .

Table 1

x	1	2	3	4	5
y	2.9	6.2	12	25	46

 (10 marks)

b) The second term of a G.D is 1.6 and the fifth term is -25. Find:

(i) The tenth term

(ii) The sum of the first ten terms

(10 marks)

Question 3

a) A project team of 5 is to be selected from 4 Engineers and 7 technicians. Find;

(i) The total number of possible teams

(ii) The number of possible selections if the team must comprise at least 1 Engineer and 2 Technicians (10 marks)

b) Given the series $10\frac{1}{2} + 12 + 13\frac{1}{2} + \dots + 27$ find;

(i) The eighth term

(ii) The sum of all the terms of the series

(10 marks)

Question 4

a) Convert the following complex numbers into polar form:

(i) $z = -3 + 45i$

(ii) $z = 5 - 25i$

(8 marks)

$$z^3 = \left(8, \frac{2\pi}{3} \right)$$

b) Use Demoivre's theorem to find z given $z^3 = \left(8, \frac{2\pi}{3} \right)$, giving your solution in the form $z = a + bj$

(12 marks)

Question 5

$$p = kq^n,$$

a) Given that $p = kq^n$ find the values of the constants k and n , if the following sets of values satisfy the relationship: $p = 20, q = 10$ and $p = 50, q = 64$.

(6 marks)

$$y = 2 + 4x - x^2$$

b) Plot the graph of $y = 2 + 4x - x^2$ for x values from -1 to $+5$ and use it to solve the equations:

(i) $4x = x^2 + 1$

(i)

(ii) $3x - x^2 + 1 = 0$

(ii)

(14 marks)