



THE MOMBASA POLYTECHNIC UNIVERSITY COLLEGE

(A Constituent College of JKUAT)

Faculty of Applied & Health Sciences

DEPARTMENT OF MATHEMATICS & PHYSICS

INSTITUTIONAL BASED PROGRAMME

UNIVERSITY EXAMINATIONS FOR DEGREE IN
BACHELOR OF SCIENCE IN ELECTRICAL & ELECTRONIC ENGINEERING
YR II, SEM II

SMA 2271: ORDINARY DIFFERENTIAL EQUATIONS

SPECIAL/SUPPLEMENTARY EXAMINATION

SERIES: FEBRUARY/MARCH 2012

TIME: 2 HOURS

Instructions to Candidates:

You should have the following for this examination

- Answer booklet

This paper consists of FIVE questions

Answer question ONE (COMPULSORY) and any other two questions

This paper consist of TWO printed pages

SECTION A (COMPULSORY)

Question One (30 Marks)

a) Explain what is a homogeneous function, hence determine the homogeneity of the function

$$f(x, y) = e^{\frac{y}{x}} + \tan \frac{y}{x}$$

(3mark)

$$e^{-3t} (2 \cos 5t - 3 \sin 3t)$$

b) Find the Laplace transform of

(5 marks)

c) Using the method of undetermined coefficient determine a general solution of an equation. (7 marks)

d) Use the method of Frobenius to find the solution of the differential equation

$$2x^2 \frac{d^2y}{dx^2} - x \frac{dy}{dx} + (x-5)y = 0$$

(12

marks)

$$\frac{dy}{dx} + y = e^x$$

- e) Find the general solution of $\frac{dy}{dx} + y = e^x$. (3 marks)

SECTION B (ANSWER ANY TWO QUESTIONS FROM THIS SECTION)

Question Two (20 Marks)

$$F(s) = \frac{3s+7}{s^2-4}$$

- a) Find the inverse Laplace transform of $F(s)$. (4 marks)

$$(3x^2 + 4xy)dx + (2x^2 + 2y)dy = 0$$

- b) Solve the equation $(3x^2 + 4xy)dx + (2x^2 + 2y)dy = 0$. (8 marks)

- c) An electric circuit consists of an inductance of 0.1 henry a resistance of 20 ohms and a condenser of capacitance 25 microfarads. Find the charge q and the current i at any time t , given that the initial

$$i = \frac{dq}{dt} = 0 \quad L \frac{d^2q}{dt^2} + R \frac{dq}{dt} + \frac{q}{C} = E(t)$$

- conditions are $q=0.05$ coulombs and $i=0$ when $t=0$ if $E(t) = 100 \sin 100t$. (8 marks)

Question Three (20 Marks)

- a) Solve $\frac{dy}{dx} + y \cot x = \cos x$ to obtain the particular solution given that at $x = \frac{\pi}{2}$, $y = \frac{5}{2}$ the $(x^2 - xy + y^2)dx - xydy = 0$. (6 marks)

- b) Obtain a general solution of the equation $(x^2 - xy + y^2)dx - xydy = 0$. (8 marks)

- c) An object moves with simple harmonic motion on the x axis. Initially it is located at a distance 46 m away from the origin when $t=0$ and has velocity $v=15$ m/s and decelerating at $100m/s^2$ directed towards the origin O. find the equation of the position at any time t . (6 marks)

Question Four (20 Marks)

$$y \tan x \frac{dy}{dx} = (4 + y^2) \sec^2 x$$

- a) a) By separation of variables solve $y \tan x \frac{dy}{dx} = (4 + y^2) \sec^2 x$. (4 marks)
- b) Find the particular solution for the initial value problem $(x^2 + y^2)dx + 2xydy = 0$ $y(1) = 1$ if $x > 0$. (8 marks)

- c) Given the equation $L \frac{di}{dt} + Ri = E(t)$, find an expression for i if $E(t) = E_0 \sin \omega t$ when the initial current is $i = 0$ provided that $L=3$ henries, $R=15$ ohms in a 60 cycle sine wave of amplitude 110volts, while $i = 0$ when $t=0$. (8 marks)

Question Five (20 marks)

- a) Find the Laplace inverse of $\frac{s+2}{s^2-4s+3}$. (5 marks)

- b) Solve the 2nd order differential equation

$$y \frac{d^2 y}{dx^2} = 2 \left[\frac{dy}{dx} \right]^2 - 2 \left[\frac{dy}{dx} \right]$$

(7 marks)

- c) A particle of mass 2kg moves along the x-axis attracted towards the origin O by a force whose magnitude is numerically equal to $8x$. if it is initially at rest at $x=20$ and has also a damping force whose magnitude is numerically equal to 8 times the instantaneous speed. Find the equations of displacement and velocity of the particle at any time t . (8 marks)