# THE MOMBASA POLYTECHNIC UNIVERSITY COLLEGE (A CONSTITUENT COLLEGE OF JKUAT) <br> Faculty of Engineering and Technology 

# DEPARTMENT OF MECHANICAL AND AUTOMOTIVE ENGINEERING DIPLOMA IN MECHANICAL ENGINEERING (PRODUCTION OPTION) <br> DIPLOMA IN MECHANICAL ENGINEERING (PLANT OPTION) DIPLOMA IN MECHANICAL ENGINEERING (AUTOMOTIVE OPTION) 

EME 2310<br>STRENGTH OF MATERIALS IV

STAGE III SEMESTER II
SPECIAL/SUPPLEMENTARY EXAMINATIONS
SERIES: MARCH, 2012
TIME: 2 HOURS

## INSTRUCTIONS TO CANDIDATES

1. You should have the following for this examination

- Answer booklet
- Scientific calculator
- Drawing instruments

2. This paper consists of FIVE questions
3. Answer any THREE questions.
4. Maximum marks per each question are shown.
5. This paper consists of THREE printed pages.

## QUESTION 1

a) With reference to Castigiliano's theorem prove the following relationship:

$$
U=\int \frac{M^{2}}{2 E I} d x
$$

Note: the variables maintain their usual meaning.
b) For a closed coil spring show that the resilience can be given by:

$$
\begin{aligned}
& u=\frac{\tau^{2}}{4 G} \quad \text { Where: } \quad u=\text { resilience } \\
& \tau=i \quad \text { Shear stress }
\end{aligned}
$$

Note: any other formulae used must be proved

## QUESTION 2

An axially loaded close-coiled spring whose free length is to be 50 mm is required to have strain energy of $\mathbf{0 . 4 5 J}$ when the maximum shearing stress is $50 \mathrm{NM} / \mathrm{m}^{2}$ and the spring is fully compressed (i.e. coils touching). Assuming a mean coil diameter 0f 25 mm , determine;
i. The diameter of the steel wire
ii. The number of coils required

Take: $G=80 G N / m^{2}$
(20 marks)

## QUESTION 3

Obtain an expression for the horizontal displacement of point A in the bent cantilever shown in figure 1 which is of breadth $b$.
If $\mathrm{r}=40 \mathrm{~mm}, \mathrm{t}=6 \mathrm{~mm}, \mathrm{~b}=20 \mathrm{~mm}, \mathrm{~h}=80 \mathrm{~mm}$ and the beam is of steel. Find the horizontal displacement of A for $\mathrm{W}=25 \mathrm{~N}$ TAKE: $E=200 G N / \mathrm{m}^{2}$
(20 marks)


## QUESTION 4

a) Deduce an expression for the central deflection of a carriage spring when simply supported at the ends and loaded in the centre so that the plates become straight.
b) Such a spring has 12 plates each 65 mm wide by 6 mm thick and the longest plate is 0.8 m long. The greatest bending stress is not to exceed $185 \mathrm{MN} / \mathrm{m}^{2}$ and the central deflection when the spring is fully loaded is not to exceed 20 mm . Determine the magnitude of the greatest central load that can e applied to the spring Take ( $E=200 \mathrm{GN} / \mathrm{m}^{2}$ ).
(20 marks)

## QUESTION 5

a) An open-coiled spring carries an axial load $\boldsymbol{W}$. derive expressions for displacement and angular twist of the free end. (12 marks)
b) For an open-coiled spring of helix angle $30^{\circ}$, determine the mean radius to give a vertical displacement of 23 mm and an angular rotation of the load end of 0.02 radians under an axial load of 35 N . The material available is steel $\operatorname{rod} 6 \mathrm{~mm}$ diameter.

Take $E=200,000 \mathrm{~N} / \mathrm{mm}^{2}: \quad G=80 \mathrm{~N} / \mathrm{mm}^{2}$.

