

TECHNICAL UNIVERSITY OF MOMBASA

Faculty of Engineering & Technology in Conjunction with Kenya Institute of Highways & Building Technology (KIHBT)

DEPARTMENT OF BULDING & CIVIL ENGINEERING

HIGHER DIPLOMA IN BUILDING ECONOMICS

EBE 3102: ENGINEERING MATHEMATICS II

END OF SEMESTER EXAMINATIONS

SERIES: APRIL 2014

TIME: 2 HOURS

INSTRUCTIONS:

- You should have the following for this examination:
 - Answer booklet
 - Mathematical table/scientific calculator
- Answer question **ONE (Compulsory)** and any other **TWO**.

This paper consists of Three printed pages.

QUESTION 1 (Compulsory)

a) Evaluate the following:

i)
$$\int_{1}^{4} \frac{et}{4 + e^{t}} dt$$
ii)
$$\int x^{2} \ln x dx$$
marks) (8

b) Find radius of curvature at the point x = 1 given function: $y = x^3 - \frac{1}{x} + \ln x + xy^2$ (12 marks)

c) Evaluate
$$\int \frac{8x}{(x^2-1)(x^2+1)^{dx}}$$
 (10 marks)

QUESTION 2

a) Evaluate
$$\int \frac{2x^3 + 1}{x(x^2 - 1)} dx$$
 (10)

marks)

b) Determine the radius of curvature for the function given as $x = \sin t$ $y = \cos 4t$ at the point where

$$t = \frac{\pi}{4}$$
 (10 marks)

QUESTION 3

a) Evaluate
$$\int \cos 2t \sin 7t dt$$
 (7 marks)

b) Find partial fractions for
$$\frac{5x+2}{x(x^2+1)}$$
 and hence evaluate $\int \frac{5x+2}{x(x^2+1)} dx$ (13 marks)

QUESTION 4

a) Evaluate:

i)
$$\int_{\frac{\pi}{6}}^{\frac{\pi}{3}} \frac{2}{3} \sin t \cos^3 t \, dt$$

ii)
$$\int \sqrt{x} \log_e x \, dx$$
 (9 marks)

b) Find the radius of curvature at the point where x = 1 for the function $y^2 = xy + \frac{1}{x}$ (11 marks)

QUESTION 5

a) Evaluate the partial fractions for:

$$\frac{4}{x^2 + 3x + 2}$$
 and hence evaluate $\int_1^3 \frac{4}{x^2 + 3x + 2} dx$ (4 marks)

- b) Evaluate $\int x^2 \cos x \, dx$ (8 marks)
- c) Determine the radius of curvature at the point where $t = \frac{\pi}{8}$ for the function defined as:

$$x = \sin 2t \quad y = \cos 2t \tag{8 marks}$$