



TECHNICAL UNIVERSITY OF MOMBASA

FACULTY OF APPLIED AND HEALTH SCIENCES
DEPARTMENT OF MATHEMATICS & PHYSICS

UNIVERSITY EXAMINATION FOR:
THE DEGREE OF BACHELOR OF
AMA4408: TOPOLOGY
SPECIAL/ SUPPLIMENTARY EXAMINATIONS

SERIES: September 2018

TIME: 2HOURS

DATE: Pick Date Sep2018

Instructions to Candidates

You should have the following for this examination

-Answer Booklet, examination pass and student ID

This paper consists of **FIVE** questions. Attempt question ONE (Compulsory) and any other TWO questions.

Do not write on the question paper.

Question ONE (30 MARKS)

- a) Let A be a subset of a topological space (X, τ) on $X = \{a, b, c\}$ Show that the derived set A' of A is empty (5 marks)
- b) Let τ be the class of subsets of \mathbb{R} consisting of \mathbb{R}, ϕ empty set and all open infinite intervals $E_n = (a, \infty)$ with a belonging to $a \in \mathbb{R}$. Show that τ is a topology on \mathbb{R} (6 marks)
- c) Define the following
 - i) open neighbourhood (3marks)
 - ii) closed set (3marks)
 - iii) cluster point (3marks)
- d) Let τ be the cofinite topology on any set X . Show that
- e) Define a normal space (2 marks)

Question TWO (20 MARKS)

a) Consider the topology on $X = \{a, b, c, d, e\}$

$$\tau = \{X, \phi, \{a\}, \{a, b\}, \{a, c, d\}, \{a, b, c, d\}, \{a, b, e\}\}$$

i) List the closed subsets of X (4 marks)

ii) Determine the closure of the set (4 marks)

$\{a\}$

$\{b\}$

$\{c, e\}$

iii) State the sets that are dense in X (2 marks)

b) State and prove Lindelof's theorem (10 marks)

Question THREE (20 MARKS)

a) Show that every subspace of a Hausdorff space is also Hausdorff (8 marks)

b) Show that every subspace of a regular space is regular (8 marks)

c) When is a topological space first countable space (2 marks)

d) State what is meant by a regular space (2 marks)

Question FOUR (20 MARKS)

a) Define the following

i) Open set (3 marks)

ii) T_1 space (3 marks)

iii) Homeomorphic space (3 marks)

iv) Derived set (3 marks)

a) Let $X = \{a, b, c, d, d, e\}$.

Determine whether or not each of the following classes of subsets of X is a topology on X

(10 marks)

$$T_1 = \{X, \phi, \{a\}, \{a, b\}, \{a, c\}\}$$

$$T_2 = \{X, \phi, \{a, b, c\}, \{a, b, d\}, \{a, b, c, d\}\}$$

$$T_3 = \{X, \phi, \{a\}, \{a, b\}, \{a, c, d\}, \{a, b, c, d\}\}$$

Question FIVE (20 MARKS)

- b) Show that a set G is open if and only if it is a neighbourhood of each of its point (4 marks)
- c) Consider the topology
 $\tau = \{X, \emptyset, \{a\}, \{c, d\}, \{a, c, d\}, \{b, c, d, e\}\}$ on X and subset $A = \{a, d, e\}$ on X
Determine the relativisation of τ on A . (6 marks)
- d) Let $f: X \rightarrow Y$ be a function from a non empty set X into a topological space (Y, U) , let τ be the class of inverses of open subsets of Y :
 $\tau = \{f^{-1}(G) : G \in U\}$. Show that τ is a topology on X (8 marks)
- e) Define a normal space (2 marks)