TECHNICAL UNIVERSITY OF MOMBASA

INSTITUTE OF COMPUTING AND INFORMATICS<br>DEPARTMENT OF COMPUTER SCIENCE \& INFORMATION TECHNOLOGY UNIVERSITY EXAMINATION FOR:<br>BACHELOR OF BUSINESS \& INFORMATION TECHNOLOGY/ BACHELOR<br>OF TECHNOLOGY IN INFORMATION TECHNOLOGY<br>EIT 4110: DISCRETE STRUCTURES<br>END OF SEMESTER EXAMINATION<br>SERIES:APRIL2016<br>TIME:2HOURS<br>DATE: Pick DateSelect MonthPick Year<br>\section*{Instructions to Candidates}<br>You should have the following for this examination<br>-Answer Booklet, examination pass and student ID<br>This paper consists of FIVE questions. Attemptquestion ONE (Compulsory) and any other TWO questions.<br>Do not write on the question paper.

## Question ONE

a) Define the following terms
i) A proposition
ii) A predicate
iii) Tautology
iv) Contradiction
b) Compute the truth table for the statement $[(p \wedge q) \vee r] \Rightarrow(\sim q)$. (8 marks)
c) State and explain the Pigeonhole principle.
(4 marks)
d) How many ways can a committee of three faculty members and two students be selected from seven faculty members and 8 students. Show your work.
e) Translate the following proposition into a sentence in English

## Question TWO

Differentiate between the following terms
a) Permutation and combination
b) Random experiment and events
c) Elementary events and compound events
d) Mutually exclusive events and complementary events
e) Open sentence and logical reasoning

## Question THREE

a) Prove that the statement $(p \rightarrow q) \vee(q \rightarrow p)$ is a tautology.
(6 marks)
b) Prove by mathematical induction that $1^{2}+2^{2}+3^{2}+\ldots+n^{2}=\frac{n(n+1)(2 n+1)}{6}$
(6 marks)
c) Given that $A=\{1,3,5,7,9,11,13,17\}, B=\{5,9,13,17\}$
i) Find $A-B$
(3 marks)
ii) Using Venn diagram to represent (i) above
(3 marks)
iii) Show using a diagram that set $B$ is a proper subset of set $A$.
(2 marks)

## Question FOUR

a) City residents were surveyed recently to determine readership of newspapers available. $50 \%$ of the residents read the morning paper, $60 \%$ read the evening paper, and $20 \%$ read both newspapers. Find the probability that a resident selected reads either the morning or evening paper or both the papers.
b) There are three factories J, K, L supplying goods to warehouses $A, B, C$ and $D$, the amount of supplies from the factories to warehouses are shown below.

| Warehouses | A | B | C | D | Total |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Factory |  |  |  |  |  |
| J | 72 | 16 | 15 | 50 | 153 |
| K | 38 | 18 | 13 | 22 | 91 |
| L | 50 | 32 | 22 | 43 | 147 |
| Total | 160 | 66 | 50 | 115 | 391 |

Find the following
i) $J \cup A$
ii) $C \cup L$
iii) $K \cup D$
c) Write down a truth table to show that $\sim(p \vee q)$ is equivalent to $(\sim p) \wedge(\sim q)$.
(6 marks)

## Question FIVE

a) A survey of 126 Kenyan students found that:

92 students are taking at least an English class
90 students are taking at least a Math class
68 students are taking at least a Science class
36 students are taking English, Math, and Science classes
68 students are taking at least English and Math classes
47 students are taking at least Math and Science classes
51 students are taking at least English and Science classes
i) Draw a Venn diagram to represent the above information.
ii) How many students are only taking an English class?
iii) How many are taking only Math and Science classes?
iv) How many students are not taking English, Math, or Science classes?
b) The table below specifies a Boolean function $f: S \times S \times S \longrightarrow S$.

| $x$ | $y$ | $z$ | $f(x, y, z)$ |
| :---: | :---: | :---: | :---: |
| 0 | 0 | 0 | 1 |
| 0 | 0 | 1 | 1 |
| 0 | 1 | 0 | 0 |
| 0 | 1 | 1 | 0 |
| 1 | 0 | 0 | 1 |
| 1 | 0 | 1 | 1 |
| 1 | 1 | 0 | 0 |
| 1 | 1 | 1 | 0 |

Give a Boolean expression corresponding to this function.

