



TECHNICAL UNIVERSITY OF MOMBASA

Faculty of Engineering and Technology
Department of Mechanical & Automotive Engineering
UNIVERSITY EXAMINATION FOR:
DIPLOMA IN MARINE ENGINEERING
EMR 2201 : ENGINEERING MATH III
SPECIAL/ SUPPLIMENTARY EXAMINATIONS
SERIES: SEPTEMBER 2018
TIME: 2 HOURS
DATE: Sep2018

Instruction to Candidates:

You should have the following for this examination

- *Answer booklet*
- *Non-Programmable scientific calculator*

This paper consists of **FIVE** questions. Attempt question **ONE** and any other **TWO** questions.

Maximum marks for each part of a question are as shown.

Do not write on the question paper.

Question ONE(30mks)

a) Evaluate $\left(\frac{1+j^3}{1-j^2}\right)^2$ (4mks)

b) Prove that $1+2\sinh^2 x = \cosh 2x$ (5mks)

c) Find the sum of the first 7 terms of the series
 $\frac{1}{2}, 1\frac{1}{2}, 4\frac{1}{2}, 13\frac{1}{2}, \dots$ (3mks)

d) Reduce the equation to quadratic and solve for x

$\frac{1}{2}(e^x + e^{-x}) = 1.5$ (8mks)

e) Express (6, 5.5 rad) in Cartesian coordinates (3mks)

f) Evaluate $(2+j^3) (-4-5j)$ (3mks)

g) Evaluate $\tanh 5.2$. (4mks)

Question TWO (20mks)

a) Evaluate $(2+j3) + (3-j4)$ using argand diagram (5mks)

b) Express $(-14+j3)^{-\frac{2}{5}}$ in polar form. Give your answer in degree and minutes (8mks)

c) Given $Ae^x + Be^{-x} = 4\cosh x - 5\sinh x$. Determine values of A and B (4mks)

d) Express the complex number $Z=2+j3$ in polar form (3 marks)

Question THREE (20mks)

a) Solve the following equation simultaneously (10mks)

$$\frac{1}{x} + \frac{2}{y} + \frac{3}{z} = 6$$

$$\frac{2}{x} + \frac{3}{y} + \frac{4}{z} = 8$$

$$\frac{3}{x} + \frac{2}{y} + \frac{2}{z} = 5$$

b) The first, twelfth and last term of an arithmetic progression are 4 , $31\frac{1}{2}$, and $376\frac{1}{2}$ respectively. Determine

i) Number of terms in the series (5mks)

ii) Sum of all terms in the series (3mks)

c) Evaluate $\sinh 1.2$ (2mks)

Question FOUR (20mks)

a) Find sum of the five terms in the series $8, -4, 2, -1, \dots$ (3mks)

b) Express in polar form leaving answers in surd form

$$(-2+j)^3 \text{ (6mks)}$$

c) Solve for x given

$$\log_4 x + \frac{4}{\log_4 x} = 5 \quad (7\text{mks})$$

d) Solve for x and y given

$$2(x+jy)=6+2j \quad (4\text{mks})$$

Question FIVE (20MKS)

A) Prove the identity $\sin 3x = 3\sin x - 4\sin^3 x$ (7mks)

b) Given $Z_1 = 1-3j$, $Z_2 = -2+j5$ and $Z_3 = -3-j4$. Determine in Cartesian form

$$\frac{Z_1 Z_3}{Z_1 + Z_2} \quad (6\text{mks})$$

C) In Geometric progression the 6^{th} term is 8 times the 3^{rd} term and sum of the 7^{th} and 8^{th} term is 192. Determine

i) The common ratio (2mks)

ii) The first term (2mks)

iii) The sum of the 5^{th} to the 11^{th} term inclusive (3mks)