# Faculty of Engineering and Technology <br> Department of Mechanical \& Automotive Engineering UNIVERSITY EXAMINATION FOR: <br> <br> BSc. Mechanical Engineering <br> <br> BSc. Mechanical Engineering <br> EMG 2403: Solids \& Structural Mechanics III SUPPLEMENTARY EXAMINATION <br> SERIES: September 2018 <br> TIME: 2 HOURS 

## Instruction to Candidates:

You should have the following for this examination

- Answer booklet
- Non-Programmable scientific calculator

This paper consists of FOUR questions. Attempt any THREE questions.
Maximum marks for each part of a question are as shown.
Do not write on the question paper.

## Question ONE

A steel cylinder of outside diameter 102 mm is shrink-fitted onto a bronze rod of diameter 64 mm and the two materials are in contact over a length a length of 60 mm . A hoop stress of magnitude $92 \mathrm{MN} / \mathrm{m}^{2}$ occurs at the outer radius of the steel cylinder.
(i) Calculate the contact pressure between the steel cylinder and the bronze rod, and calculate also the force that would be needed to pull out the steel cylinder from the bronze rod.
(ii) Calculate the difference in diameters of the mating surfaces before assembly.

$$
\begin{aligned}
& E_{\text {steel }}=200 \mathrm{GN} / \mathrm{m}^{2} \\
& v_{\text {steel }}=0.29 \\
& E_{\text {bronze }}=100 G N / \mathrm{m}^{2} \\
& v_{\text {bronze }}=0.34 \\
& \mu_{0}=0.3 \\
& E=\text { Modulus of Elasticity of the materials } \\
& v=\text { Poisson's ratio of the materials } \\
& \mu_{0}=\text { Coefficient of friction between the two surfaces }
\end{aligned}
$$

## Question TWO

Fig Q2 shows a bracket in the form of a curved beam, fixed at the top and supporting a point load $W$ as well as an anti-clockwise couple of magnitude 1.6 Wa . The cross-
section of the beam is also indicated with the dimensions given as functions of ' $a$ '. Derive expressions for the Maximum Tensile Stress and the Maximum Compressive Stress at section $x-y$.

## Question THREE

Fig Q3 shows a cross-section of a cantilever beam of length $16 a$ fixed at one end and supporting a vertical downward acting load of magnitude $W$ at the free end.
Derive expressions for the Maximum Tensile Stress and the Maximum Compressive Stress at the fixed end.

## Question FOUR

A steel rotor of outside diameter 800 mm and inside diameter 400 mm has rotor blades evenly distributed on the outside diameter, each with a mass of 0.1 kg and at an effective radius of 450 mm . If while rotating at a speed of 3000 rpm , a maximum Hoop Stress of $380 \mathrm{MN} / \mathrm{m}^{2}$ is obtained, calculate the number of blades on the rotor.
The expressions for the variation of the Radial Stress $\left(\sigma_{r}\right)$ and Hoop Stress ( $\sigma_{H}$ ) are given by the relationships:

$$
\begin{gathered}
\sigma_{r}=A-\frac{B}{r^{2}}-\left(\frac{3+v}{8}\right) \rho w^{2} r^{2} \\
\sigma_{H}=A+\frac{B}{r^{2}}-\left(\frac{1+3 v}{8}\right) \rho w^{2} r^{2}
\end{gathered}
$$

where $A$ and $B$ are constants, $E=200 G N / \mathrm{m}^{2} ; \rho=7830 \mathrm{~kg} / \mathrm{m}^{3} ; v=0.3$ $E=$ Modulus of Elasticity of the material $\rho=$ Density of the material $v=$ Poisson's ratio of the material

## Question FIVE

Fig Q5 shows a beam of thin cross-section, breadth ' $b$ ' and thickness ' $t$ ', fixed at the top and supporting a load $W$ at the free end. The load is applied on a block that is constrained to move in a vertical direction by vertical guides with smooth surfaces. If $b=20 \mathrm{~mm}, t=6 \mathrm{~mm}, R=200 \mathrm{~mm}$ and $W=120 \mathrm{~N}$, calculate the magnitude of the vertical deflection $E=210 G N / \mathrm{m}^{2}$



