TECHNICAL UNIVERSITY OF MOMBASA

## Faculty of Engineering E Jechnolagy

DEPARTMENT OF MECHANICAL \& AUTOMOTIVE ENGINEERING
UNIVERSITY EXAMINATIONS
FOR THE DEGREE OF BACHELOR OF SCIENCE IN MECHANICAL ENGINEERING
EMG 2301 FLUID MECHANICS II
SUPPLEMENTARY/SPECIAL EXAMINATION
SERIES: SEPTEMBER 2018
TIME: 2 HOURS

## INSTRUCTIONS TO CANDIDATES:

1. You should have Answer Booklet for this examination.
2. This paper contains FIVE questions. Answer ANY THREE questions.
3. All diagrams should be clearly drawn and labeled.
4. This paper consists of SEVEN printed pages.

## Question 1

1. A pipe bends through $90^{\circ}$ from its initial direction. The pipe reduces in diameter such that the velocity at point (2) is 1.5 times the velocity at point (1). The pipe is 200 mm diameter at point (1) and the static pressure is 100 kPa . The volume flow rate is $0.2 \mathrm{~m}^{3} / \mathrm{s}$. Assume there is no friction and the weight of the bend and water is negligible. Calculate the following.
(a) The static pressure at (2).
(b) The velocity at (2).
(c) The horizontal and vertical forces on the bend $\mathrm{F}_{\mathrm{H}}$ and $\mathrm{F}_{\mathrm{v}}$.
(d) The total resultant force on the bend.

## Question 2

(a) Derive the expression for the loss of head at a sudden expansion and show that this may also be used to approximate to the loss through a sudden contraction.
(b) A 150 mm diameter pipe reduces in diameter abruptly to 100 mm diameter. If the pipe carries water at $30 \mathrm{~L} / \mathrm{s}$, calculate the pressure loss across the contraction and express this as a percentage of the loss to be expected if the flow was reversed. Take the coefficient of contraction as 0.6.
(c) A pipeline that transports oil at $40^{\circ} \mathrm{C}$ at a rate of $3 \mathrm{~m}^{3} / \mathrm{s}$ branches into two parallel pipes made of commercial steel that reconnect downstream. Pipe A is 500 m long and has a diameter of 30 cm while pipe B is 800 long and has a diameter of 45 cm . The minor losses are considered to be negligible. Calculate the flow rate through each of the parallel pipes.

## Question 3

(a) Water main 0.6 m in diameter discharges $0.45 \mathrm{~m}^{3} / \mathrm{s}$. The surface of the pipe is rough and may be taken as having protuberances of effective height of 1.25 mm . Calculate the loss of head per unit length. Calculate also the loss of head per unit length in an 18 mm diameter pipe of the same material in which water at $15^{\circ} \mathrm{C}$ is flowing at a velocity of 1.5 $\mathrm{m} / \mathrm{s}$.
(b) A thin oil having density of $800 \mathrm{~kg} / \mathrm{m}^{3}$ is pumped through a 300 mm pipeline 6.3 km long; the coefficient of viscosity of the oil is 0.01865 poises. The roughness of the inner surface of the pipe is such that the mean height of the roughness projections is 0.75 mm . The quantity of flow through the pipe is $0.22 \mathrm{~m}^{3} / \mathrm{s}$. Using the roughness coefficient curves, calculate the head lost in $\mathrm{N} / \mathrm{m}^{2}$ and the power required to drive the pump if the overall efficiency of the pump is $75 \%$.

## Question 4

(a) A steel circular pipeline of diameter 1.4 m has water flowing at a half-full. The pipeline is at gradient $1 / 250$. Calculate the discharge from the pipe, Q ?
(5 marks)
(b) Water is to be transported in an open-channel whose surfaces are asphalt lined at a rate of $4 \mathrm{~m}^{3} / \mathrm{s}$ in uniform flow. The bottom slope is 0.0015 . Calculate the dimensions of the best cross-section if the shape of the channel is;
(i) Circular diameter $D$
(ii) Rectangular of bottom width $b$,
(iii) Trapezoidal of bottom $b$.

## Question 5

(a) Show by dimensional analysis that the power $P$ required to operate a test tunnel is given by

$$
P=\rho L^{3} V^{3} f\left(\frac{\mu}{\rho L V}\right)
$$

where $\rho$ is the density and $\mu$ the coefficient of dynamic viscosity of the fluid $V$ the linear velocity of the fluid relative to the tunnel and $L$ the characteristic linear dimension of the tunnel.
(12 marks)
(b) A water tunnel was constructed for visual observation of the flow past models. It operates with the water flowing at a velocity of $3 \mathrm{~m} / \mathrm{s}$ in the working section and absorbs 3.75 kW . If it is to operate as a wind tunnel under dynamically similar conditions, determine (a) the corresponding speed of air in the working section, and (b) the power required. Assume that for water $\rho=1000 \mathrm{~kg} / \mathrm{m}^{3}$ and kinematic viscosity $v=1.14 \times 10^{-6} \mathrm{~m}^{2} / \mathrm{s}$, for air $\rho=1.28$ $\mathrm{kg} / \mathrm{m}^{3}, v=14.8 \times 10^{-6} \mathrm{~m}^{2} / \mathrm{s}$.

## APPENDIX



Figure 1: Moody chart - Variation of friction factor ( $f$ ) with Reynolds number (Re) and pipe wall roughness $(\varepsilon / D)$ for ducts of circular cross-section

Table 1: Equivalent sand-grain roughness ( $k_{s}$ ) for various pipe materials* From Crowe and Elger (2009)

| Boundary layer material | $k_{\mathrm{s}}$, millimetres |
| :--- | :--- |
| Glass, plastic | smooth |
| Copper or brass tubing | 0.0015 |
| Wrought iron, steel | 0.046 |
| Asphalted cast iron | 0.12 |
| Galvanized iron | 0.15 |
| Cast iron | 0.26 |
| Concrete | 0.3 to 3.0 |
| Riveted steel | 0.9 to 9.0 |
| Rubber pipe (straight) | 0.025 |

Table 2: Experimentally determined mean values of Manning coefficient $n$ for water flow in open channels* From Chow (1959).

| Wall material | n |
| :---: | :---: |
| A. Artificially lined channels |  |
| Glass | 0.010 |
| Brass | 0.011 |
| Steel, smooth | 0.012 |
| Steel, painted | 0.013 |
| Steel, riveted | 0.015 |
| Cast iron | 0.013 |
| Concrete, finished | 0.012 |
| Concrete, unfinished | 0.014 |
| Wood, planed | 0.012 |
| Wood, unplanned | 0.013 |
| Clay tile | 0.014 |
| Brickwork | 0.015 |
| Asphalt | 0.016 |
| Corrugated metal | 0.022 |
| Rubble masonry | 0.025 |
| B. Excavated earth channels |  |
| Clean | 0.022 |
| Gravelly | 0.025 |
| Weedy | 0.030 |
| Stonny, cobbles | 0.035 |
| C. Natural channels |  |
| Clean and straight | 0.030 |
| Sluggish with deep pools | 0.040 |
| Major rivers | 0.035 |
| Mountain streams | 0.050 |
| D. Floodplains |  |
| Pasture farmland | 0.035 |
| Light bush | 0.050 |
| Heavy bush | 0.075 |
| Trees | 0.150 |

Table 3: List of Dimensions Associated with Common Physical Quantities From Crowe and Elger (2009).

|  |  | Dimensions |  |
| :---: | :---: | :---: | :---: |
| Physical |  | FLT | MLT |
| Quantity | Symbol | System | System |
| Acceleration | $d V / d t$ | $L T^{-2}$ | $L T^{-2}$ |
| Angle | $\theta$ | $F^{\circ} L^{0} T^{\text {o }}$ | $M^{\circ} L^{\circ} T^{\text {o }}$ |
| Angular acceleration | $\dot{\omega}$ | $T^{-2}$ | $T^{-2}$ |
| Angular velocity | $\omega, \Omega$ | $T^{-1}$ | $T^{-1}$ |
| Area | A | $L^{2}$ | $L^{2}$ |
| Density | $\rho$ | $F L^{-4} T^{2}$ | $M L^{-3}$ |
| Energy | E | $F L$ | $M L^{2} T^{-2}$ |
| Force | $F$ | $F$ | $M L T^{-2}$ |
| Frequency | $v$ | $T^{-1}$ | $T^{-1}$ |
| Heat | $Q$ | $F L$ | $M L^{2} T^{-2}$ |
| Length | $L$ | L | L |
| Mass | M | $F L^{-1} T^{2}$ | M |
| Mass flow | $\dot{m}$ | $F L^{-1} T$ | $M T^{-1}$ |
| Modulus of elasticity |  | $F L^{-2}$ | $M L^{-1} T^{-2}$ |
| Moment of a force |  | $F L$ | $M L^{2} T^{-2}$ |
| Moment of inertia (area) |  | $L^{4}$ | $L^{4}$ |
| Moment of inertia (mass) |  | $F L T{ }^{2}$ | $M L^{2}$ |
| Momentum | M | $F L$ | $M L^{2} T^{-2}$ |
| Power | $P$ | $F L T^{-1}$ | $M L^{2} T^{-3}$ |
| Pressure | $p$ | $F L^{-2}$ | $M L^{-1} T^{-2}$ |
| Specific heat | $c_{\mathrm{p},} c_{\mathrm{v}}$ | $L^{2} T^{-2} \theta^{-1}$ | $L^{2} T^{-2} \theta^{-1}$ |
| Specific weight | $\gamma$ | $F L^{-3}$ | $M L^{-2} T^{-2}$ |
| Speed of sound | $a$ | $L T^{-1}$ | $L T^{-1}$ |
| Strain | $\epsilon$ | $F^{\circ} L^{\circ} T^{\text {o }}$ | $F^{o} L^{\circ} T^{\text {o }}$ |
| Strain rate | $\dot{\varepsilon}$ | $T^{-1}$ | $T^{-1}$ |
| Stress | $\sigma, \tau$ | $F L^{-2}$ | $M L^{-1} T^{-2}$ |
| Surface tension | Y | $F T^{-1}$ | $M T^{-2}$ |
| Temperature | $T$ | $\theta$ | $\theta$ |
| Time | T | T | T |


| Thermal conductivity | $k$ | $F L T^{-1} \theta^{-1}$ | $M L T^{-3} \theta^{-1}$ |
| :--- | :--- | :--- | :--- |
| Thermal expansion coefficient | $\beta$ | $\theta^{-1}$ | $\theta^{-1}$ |
| Torque | $T$ | $F L$ | $M L^{2} T^{-2}$ |
| Velocity | $V$ | $L T^{-1}$ | $L T^{-1}$ |
| Viscosity (dynamic) | $\mu$ | $F L^{-2} T$ | $M L^{-1} T^{-1}$ |
| Viscosity (kinematic) | $v$ | $L^{2} T^{-1}$ | $L^{2} T^{-1}$ |
| Volume | Q | $L^{3}$ | $L^{3}$ |
| Volume flow | $\dot{Q}$ | $L^{3} \mathrm{~T}^{-1}$ | $L^{3} \mathrm{~T}^{-1}$ |
| Work | $W$ | $F L$ | $M L^{2} T^{-2}$ |

