TECHNICAL UNIVERSITY OF MOMBASA

# FACULTY OF APPLIED AND HEALTH SCIENCES <br> DEPARTMENT OF MATHEMATICS \& PHYSICS <br> UNIVERSITY EXAMINATION FOR: <br> UPGRADING MATHEMATICS 

AMA 1101: ALGEBRA
SPECIAL/ SUPPLIMENTARY EXAMINATIONS
SERIES: SEPTEMBER 2018
TIME:2HOURS
DATE: Pick DateSep2018

## Instructions to Candidates

You should have the following for this examination
-Answer Booklet, examination pass and student ID
This paper consists of FIVE questions. Attempt question ONE (Compulsory) and any other TWO questions.
Do not write on the question paper.

## Question ONE

a). Express in logarithmic form $x^{m}=b$
(2 marks)
b). Express $\frac{\sqrt{5}-2 \sqrt{3}}{\sqrt{3}+\sqrt{5}}$ in the form $a+b \sqrt{c}$ where a ,b, and c are real numbers. (4 marks)
c). Express $13 \frac{3}{8}$ in binary form
d). Simplify $\sqrt{50}+\sqrt{2}-2 \sqrt{18}+\sqrt{8}$ (5 marks).
e).Evaluate $\quad \frac{\frac{9}{4}+\frac{7}{3}}{4} \times \frac{4}{\frac{13}{4}-\frac{7}{3}}$ (4marks)
f). Make x the subject $\frac{5}{2 x+5}=\frac{3}{x+4}$ (3 marks).
g). Find the common ratio and sum of the series $\frac{1}{3}+\frac{1}{9}+\frac{1}{27} \ldots \ldots$.
h). Determine how many different arrangements can be made using 5 letters of the word POWDERY.

## Question TWO

a).Expand the function $(1-2 x)^{5}$ upto the $3^{\text {rd }}$ term, hence find the value of $(0.98)^{5}$ correct to 3 decimal places.
b). Solve for x using completing the square method $2 x^{2}+9 x-5=0$
c). Find $\mathrm{x}, \log (4-2 x)=\log (x+3)+2 \log 2$
d). Find $\quad 9 c_{3}+8 p_{3}$
(3marks)

## Question THREE

a). Determine the type of the series $8+5+2 \ldots$ And hence find the sum of the first 15 terms. ( 6 marks).
b).Draw the graph of y against x and determine the law connecting the variables

| x | 0.2 | 0.4 | 0.6 | 0.8 |
| :--- | :--- | :--- | :--- | :--- |
| y | 0.4 | 3.2 | 10.8 | 25.6 |

From the graph determine the value of $y$ if $x=0.5$ and $x$ if $y=15$.
c).convert into a fraction $11.1 \dot{4} \dot{5}$
d). Simplify $a b^{2}+6 a^{2} b+10 a^{2} b-6 a b^{2}$

## Question FOUR

a). Express as a simplified single fraction $\frac{x+3}{4}+\frac{2-x}{3}-\frac{1}{2}$
(4marks)
b).Express $\quad \log _{c} \frac{\sqrt{b^{2} c^{n}}}{3 \sqrt{d}} \quad$ in single logarithms
(4marks).
c).The square of $y$ varies directly as the cube of $x$, When $x=0.4$ and $y=3.2$, find the equation relating $x$ and $y$.
d).ALI and Juma shares some money such that ALI gets $60 \%$ of the total. If Ali's amount was ksh. 2000 more than what Juma got. Determine the total amount of money shared.
(5marks)
e).Make x the subject $\quad y=\sqrt{\frac{x-2}{y-x}} \quad$ and determine x if $\mathrm{y}=2$

## Question FIVE

a). Solve the pair of simultaneous equations

$$
\begin{aligned}
& 6 x+7 y=5 \\
& 5 x+3 y=7
\end{aligned}
$$

b).Factorize completely $\left(2 y^{2}-y-10\right) \div(y+2)$ (4marks)
c). Show that $a y^{2}+b y+c=0$ can be expressed in the form $y=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}$ (9 marks)
d). Find $\mathrm{m} ; \quad\left(\frac{1}{27}\right)^{m} \times 81^{-m}=(243)^{\frac{3}{2}}$

