



# TECHNICAL UNIVERSITY OF MOMBASA

Faculty of Engineering and Technology

Department of Mechanical and Automotive Engineering

## UNIVERSITY EXAMINATION FOR:

Diploma in Chemical Engineering

ECI 2230: CONTROL SYSTEMS I

END OF SEMESTER EXAMINATION

**SERIES: SEPTEMBER 2018**

**TIME: 2 HOURS**

**DATE: Sep 2018**

### Instructions to Candidates

You should have the following for this examination

-Answer Booklet, examination pass and student ID

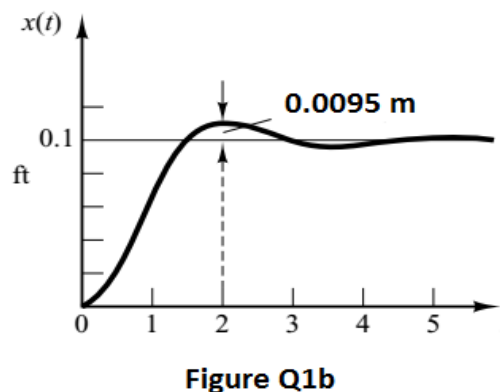
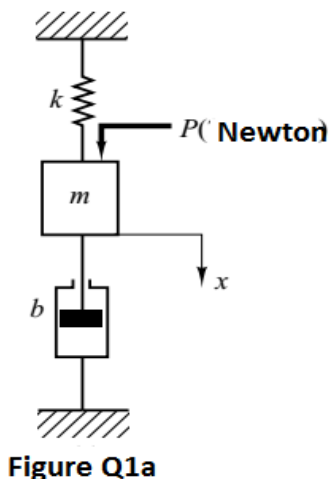
This paper consists of **five** Questions; Question ONE is compulsory. In addition attempt any Other TWO Questions.

**Do not write on the question paper.**

### Question ONE (Compulsory 30 marks)

- a) When the system of Figure Q1a is subjected to a unit step input of  $P = 2$  Newton, the system output oscillates as in Figure Q1b. Determine the values of  $m$ ,  $b$  and  $k$  from the response curve.

(8 marks)



b) A system is describe by the following equation

$$\frac{d^2y}{dt^2} + 8\frac{dy}{dt} + 25y(t) = 50x(t)$$

Evaluate the response and maximum output for a step of 2.5 units

(15 marks)

c) Given the following characteristic equation, determine the value of K for stability

(7 marks)

$$s^4 + Ks^3 + s^2 + s + 1 = 0$$

### Question TWO

a) Determine the transfer function  $X_2(S)/U(S)$

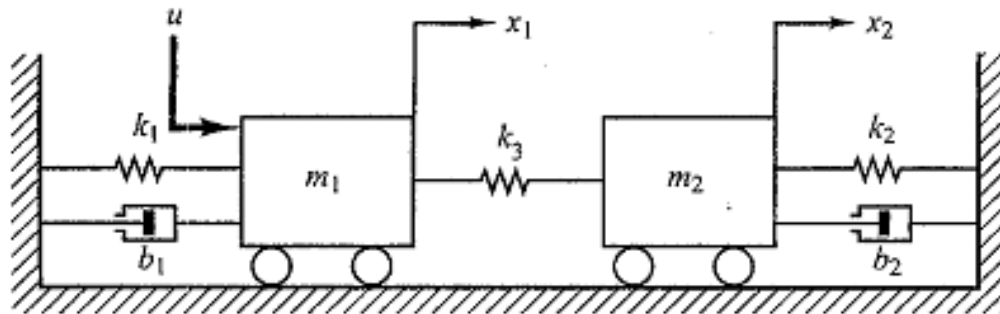


Figure 1

(12 marks)

b) Obtain the signal from diagrams from the following equations

$$x_1 = a_{11}x_1 + a_{12}x_2 + a_{13}x_3 + b_1u_1$$

$$x_2 = a_{21}x_1 + a_{22}x_2 + a_{23}x_3$$

$$x_3 = a_{31}x_1 + a_{32}x_2 + a_{33}x_3$$

(8 marks)

### Question THREE

- a) The liquid level system of Figure Q3a has an outflow rate  $Q$  m<sup>3</sup>/ Sec through the outflow valve related to the head  $H$  by

$$Q = K\sqrt{H} = 0.01\sqrt{H}$$

Assume that when the inflow rate  $Q_i$  is 0.015 m<sup>3</sup>/sec the head stays constant. For  $t < 0$  the system is at steady state ( $Q_i = 0.015$  m<sup>3</sup>/sec). At  $t = 0$  the inflow valve is closed so there is no inflow for  $t \geq 0$ . Find the time necessary to empty the tank to half the original head. The capacitance of the tank is 2 m<sup>2</sup>

(12 marks)

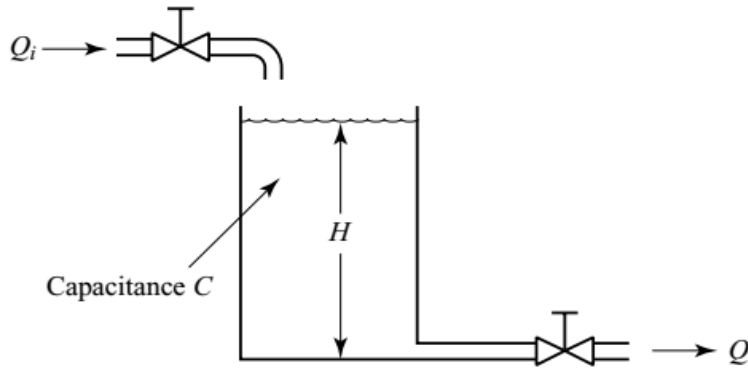


Figure Q3a

- b) Using Obtain the equivalent spring constants for the systems in Figure Q3bi and Figure Q3bii

(8 marks)

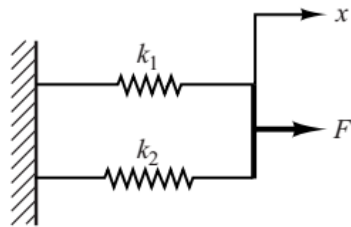


Figure Q3bi

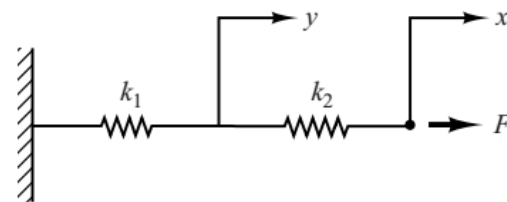


Figure Q3b ii

#### Question FOUR

- a) Using block diagram algebra, reduce the block diagram of Figure Q4a and obtain the closed loop transfer function

(10 marks)

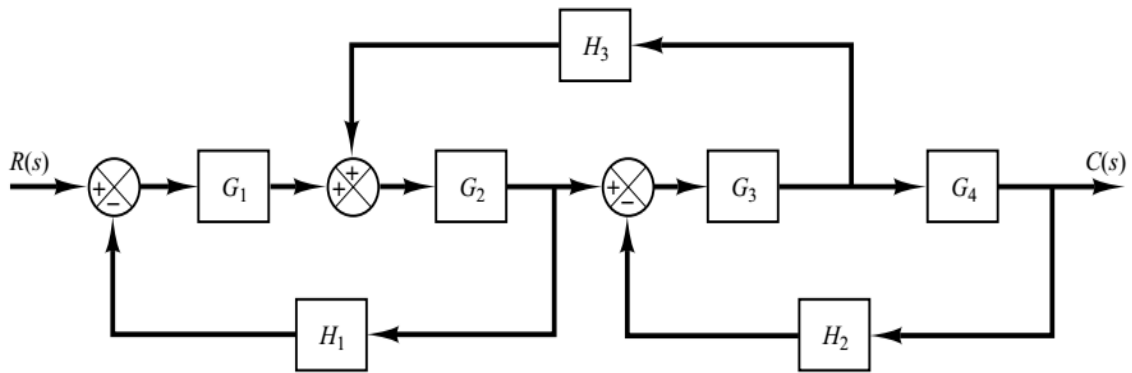


Figure Q4a

- b) Obtain the closed loop transfer function of the system of Figure Q4b using masons gain Formula (10 marks)

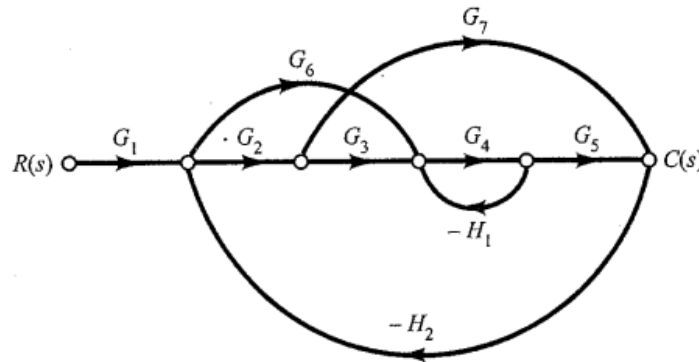


Figure Q4b

### Question FIVE

- a) For the transfer function  $G(s)$  given below, sketch an open loop frequency response locus on a Nichols chart

From the sketch, determine:

- i) The phase margin
- ii) The gain margin
- iii) Phase crossover frequency
- iv) Gain crossover frequency
- v) Bandwidth

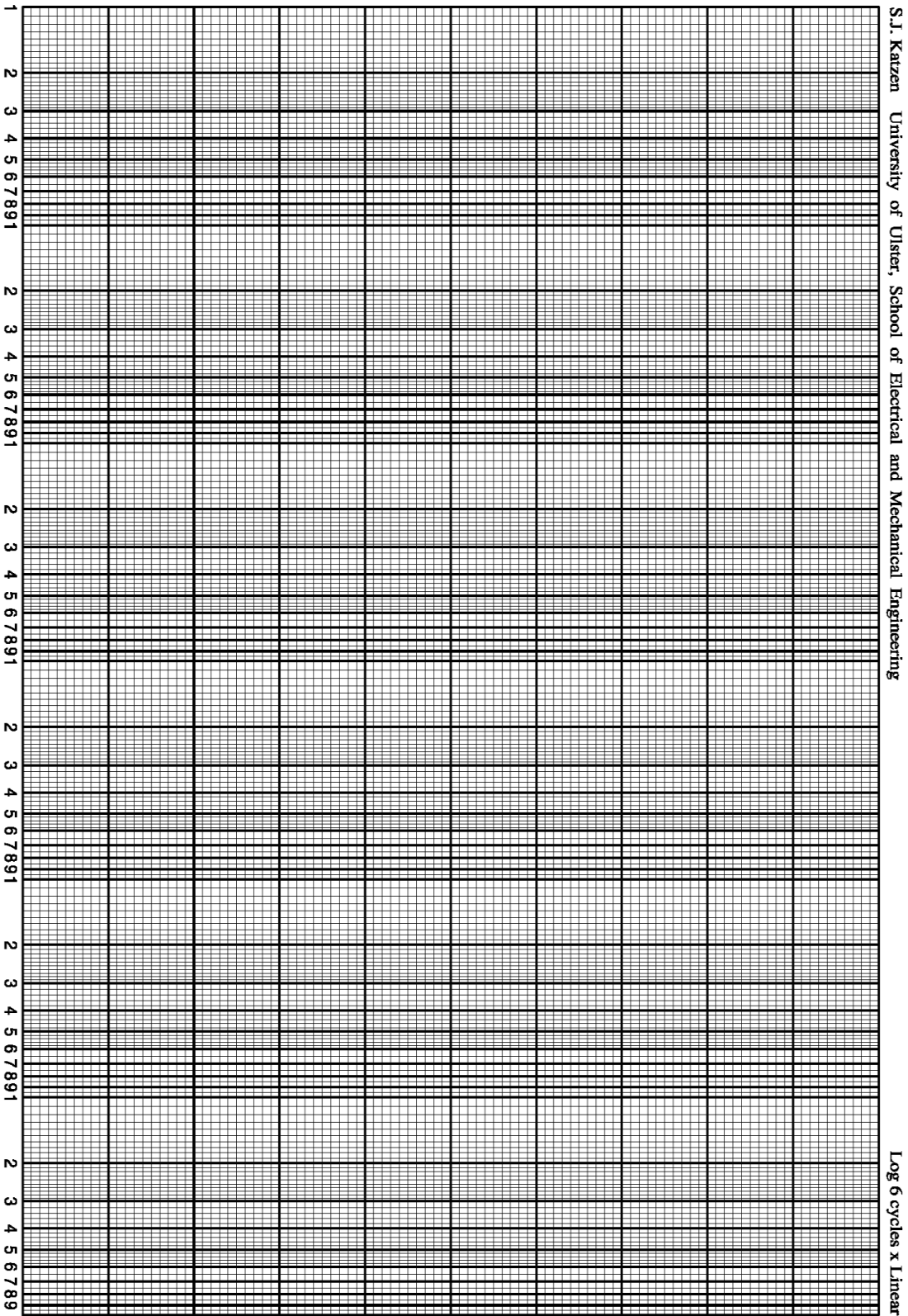
$$G(s) = \frac{1}{s(s+1)(0.5s+1)}$$

(14 marks)

- a) Explain the following terms.

- i) Disturbances
- ii) Plants
- iii) Systems

(6 marks)



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Log 6 cycles x Linear

