TECHNICAL UNIVERSITY OF MOMBASA

## FACULTY OF HEALTH AND APPLIED SCIENCES DEPARTMENT OF MATHEMATICS AND PHYSICS

# UNIVERSITY EXAMINATION FOR: <br> UPGRADING MATHEMATICS 

AMA 1001: ALGEBRA
END OF SEMESTER EXAMINATION

## SERIES: DECEMBER 2016

TIME: 2 HOURS

## Instructions to Candidates

You should have the following for this examination
-Answer Booklet, examination pass and student ID
This paper consists of five questions.
Attempt question ONE compulsory and ANY other Two questions
Do not write on the question paper.

Question ONE (30 marks)
a) Transpose the formulae below to make $p$ the subject.

$$
\begin{equation*}
k / r=\sqrt{\frac{f+p}{f-p}} \tag{4mks}
\end{equation*}
$$

b) Derive the quadratic formulae and hence solve the equation below

$$
\begin{equation*}
3 x^{2}-14 x+8=0 \tag{7mks}
\end{equation*}
$$

c) Solve for the unknowns in the following set of equations below.

$$
\begin{aligned}
& \frac{3 r+2}{5}-\frac{2 s-1}{4}=\frac{11}{5} \\
& \frac{3+2 r}{4}+\frac{5-s}{3}=\frac{15}{4}
\end{aligned}
$$

(5mks)
d) Solve for $x$ in the equation
i. $\quad \log _{8} x=-4 / 3$ (3mks)
ii. $\quad X^{0.25}=0.792$
(4mks)
iii. $\quad 8+4(x-1)-5(x-3)=2(5-2 x)$
(3mks)
e) Determine how much of copper and how much zinc is needed to make a 99 kg brass ingot, if they have to be in the proportion copper: zinc 8:3 respectively ( 2 mks )
f) If 3 people can complete a task in 4 hours, how long will it take 5 people to complete the same task assuming rate of work remains the same. ( 2 mks )

## SECTION B

## Question TWO (20 MARKS)

a) Solve the equation given below

$$
\begin{equation*}
5.4^{x+3} \times 8.2^{2 x-1}=4.8^{3 x} \tag{6mks}
\end{equation*}
$$

b) $\quad 7\left(14.3^{x+5}\right) \times 6.4^{2 x}=294$
(6mks)

$$
\text { c) } \frac{\left(3^{2}\right)^{\frac{3}{2}} \times\left(8^{\frac{1}{3}}\right)^{2}}{(3)^{2} \times\left(4^{3}\right)^{\frac{1}{2}} \times(9)^{-\frac{1}{2}}}
$$

(3mks)
d) solve the equation

$$
\begin{equation*}
\log (x-1)+\log (x+1)=2 \log (x+2) \tag{5mks}
\end{equation*}
$$

## Question THREE (20 MARKS)

a) Simplify the expression
$K=2.76 \times(8.45+3.14)+3.45^{2}-4.89 \div 2.18$
(3mks)
b) solve for the unknown
(i). $\frac{1}{3 a-2}+\frac{1}{5 a+3}=0$
(3mks)
(ii). $\frac{3 \sqrt{t}}{1-\sqrt{t}}=-6$
(iii). $\frac{2 y}{5}+\frac{3}{4}+5=\frac{1}{20}-\frac{3 y}{2}$
(3mks)
c) Solve following quadratic equation
i. By completing square correct to 3 decimal places

$$
4.6 x^{2}+3.5 x-1.75=0
$$

ii. By factorization

$$
\begin{equation*}
3 x^{2}-11 x-4=0 \tag{4mks}
\end{equation*}
$$

## Question FOUR (20 MARKS)

a) Convert the following binary numbers into decimal number
i. $\quad 10111.00111_{2}$
(3 mks)
ii. $\quad 101101.11001_{2}$
(3 mks)
b) Convert decimal numbers into binary numbers
i. $\quad 58.3125_{10}$
(3 mks)
ii. $\quad 51.34375_{10}$
(3 mks)
c) Evaluate
i. $\quad{ }^{10} C_{6}$
ii. $\quad{ }^{7} C_{2}$
(2mks)
(2mks)
d) Evaluate
i. $\quad{ }^{9} P_{6}$
(2mks)
ii. $\quad{ }^{8} P_{3}$
(2mks)

## Question FIVE (20 MARKS)

a) Expand using Pascal's triangle

$$
(2 p-3 q)^{5}
$$

b) The $6^{\text {th }}$ term of an AP is 17 and the $13^{\text {th }}$ term is 38 .determine the $19^{\text {th }}$ term (3mks)
c) Find the 15 th term of an AP if the $1^{\text {st }}$ term is 2.5 and the $16^{\text {th }}$ term is 16
d) The $1^{\text {st }}, 12^{\text {th }}$, and the last term of an AP is 4,31 , and 376.5 respectively. Determine the number of terms in the series, the sum of all terms and the $80^{\text {th }}$ term (5mks)
e) Find the sum to infinity of the series $3,1,1 / 3 \ldots \ldots . . .$. (2 mkS)
f) The $1^{\text {st }}$ term of a GP is 12 and the $5^{\text {th }}$ term is 55 . determine the $8^{\text {th }}$ and $11^{\text {th }}$ term. ( 3 mks )

