

# TECHNICAL UNIVERSITY OF MOMBASA FACULTY OF HEALTH AND APPLIED SCIENCES DEPARTMENT OF MATHEMATICS AND PHYSICS

## **UNIVERSITY EXAMINATION FOR:**

**UPGRADING MATHEMATICS** 

AMA 1001: ALGEBRA

END OF SEMESTER EXAMINATION

**SERIES: DECEMBER 2016** 

TIME: 2 HOURS

## **Instructions to Candidates**

You should have the following for this examination *-Answer Booklet, examination pass and student ID* This paper consists of five questions.

Attempt question ONE compulsory and ANY other Two questions

Do not write on the question paper.

#### **Question ONE (30 marks)**

a) Transpose the formulae below to make p the subject.

$$\frac{k}{r} = \sqrt{\frac{f+p}{f-p}} \tag{4 mks}$$

b) Derive the quadratic formulae and hence solve the equation below

$$3x^2 - 14x + 8 = 0 (7 mks)$$

c) Solve for the unknowns in the following set of equations below.

$$\frac{3r+2}{5} - \frac{2s-1}{4} = \frac{11}{5}$$

$$\frac{3+2r}{4} + \frac{5-s}{3} = \frac{15}{4}$$
 (5mks)

d) Solve for x in the equation

i. 
$$\log_8 X = -\frac{4}{3}$$
 (3mks)

ii. 
$$X^{0.25}=0.792$$
 (4mks)

iii. 
$$8 + 4(x-1) - 5(x-3) = 2(5-2x)$$
 (3mks)

- e) Determine how much of copper and how much zinc is needed to make a 99kg brass ingot, if they have to be in the proportion copper: zinc 8:3 respectively (2 mks)
- f) If 3 people can complete a task in 4 hours, how long will it take 5 people to complete the same task assuming rate of work remains the same. (2 mks)

#### **SECTION B**

#### **Question TWO (20 MARKS)**

a) Solve the equation given below

$$5.4^{x+3} \times 8.2^{2x-1} = 4.8^{3x}$$
 (6mks)

b) 
$$7(14.3^{x+5}) \times 6.4^{2x} = 294$$
 (6mks)

$$\frac{\left(3^{2}\right)^{\frac{3}{2}} \times \left(8^{\frac{1}{3}}\right)^{2}}{\left(3\right)^{2} \times \left(4^{3}\right)^{\frac{1}{2}} \times \left(9\right)^{-\frac{1}{2}}}$$
c) (3mks)

d) solve the equation

$$\log(x-1) + \log(x+1) = 2\log(x+2)$$
 (5mks)

### **Question THREE (20 MARKS)**

a) Simplify the expression

$$K=2.76 \times (8.45 + 3.14) + 3.45^2 - 4.89 \div 2.18$$
 (3mks)

b) solve for the unknown

(i). 
$$\frac{1}{3a-2} + \frac{1}{5a+3} = 0$$
 (3mks)

$$\frac{3\sqrt{t}}{1-\sqrt{t}} = -6$$
 (3mks)

(iii). 
$$\frac{2y}{5} + \frac{3}{4} + 5 = \frac{1}{20} - \frac{3y}{2}$$
 (3mks)

c) Solve following quadratic equation

i. By completing square correct to 3 decimal places

$$4.6x^2 + 3.5x - 1.75 = 0 (4 mks)$$

ii. By factorization

$$3x^2 - 11x - 4 = 0 (4mks)$$

#### **Question FOUR (20 MARKS)**

a) Convert the following binary numbers into decimal number

b) Convert decimal numbers into binary numbers

c) Evaluate

i.  $^{10}C_6$ 

(2mks)

ii.  ${}^{7}C_2$ 

(2mks)

d) Evaluate

i.  ${}^{9}P_{6}$ 

(2mks)

ii.  $^8P_3$ 

(2mks)

# **Question FIVE (20 MARKS)**

a) Expand using Pascal's triangle

(5 mks

- b) The  $6^{th}$  term of an AP is 17 and the  $13^{th}$  term is 38.determine the  $19^{th}$  term (3mks)
- c) Find the 15th term of an AP if the 1st term is 2.5 and the 16th term is 16 (2mks)
- d) The 1<sup>st</sup>, 12<sup>th</sup>, and the last term of an AP is 4, 31, and 376.5 respectively. Determine the number of terms in the series, the sum of all terms and the 80<sup>th</sup> term (5mks)
- e) Find the sum to infinity of the series 3, 1, 1/3.......... (2 mkS)
- f) The 1<sup>st</sup> term of a GP is 12 and the 5<sup>th</sup> term is 55.determine the 8<sup>th</sup> and 11<sup>th</sup> term. (3mks)