

## TECHNICAL UNIVERSITY OF MOMBASA

## FACULTY OF ENGINEERING AND TECHNOLOGY

## DEPARTMENT OF BUILDING \& CIVIL ENGINEERING

KIBIT EXAMINATIONS FOR:
HIGHER DIPLOMA IN BUILDING AND CIVIL ENGINEERING (BUILDING ECONOMICS OPTION)

EBC 3201: MATHEMATICS III
YEAR 2 SEMESTER I
SERIES: DECEMBER 2017
TIME: 2 HOURS

## Instructions to Candidates

You should have the following for this examination
-Answer Booklet, examination pass and student ID
-Pocket calculator
This paper consists of FIVE questions. Attempt any THREE questions.
Do not write on the question paper.
Mobile Phones are NOT allowed inside the examination room.

## QUESTION ONE

(a) Determine area bounded by the function $y=12-x^{2}$ and the $x$-axis.
(b) Solve the equation $\left(2+\mathrm{x}^{2}\right) \frac{d y}{d x}=2+\mathrm{y}^{2}$ if the equation passes through point $(1,5)$.
(b) The area bounded by the function $y=x^{2}-3$ and $x$-axis is to be rotated about $x$-axis through 1 revolution. Find the volume for the solid to be generated.

## QUESTION TWO

(a) Solve the following equation:

$$
\begin{equation*}
(\mathrm{x}+\mathrm{y}) \frac{d y}{d x}=\mathrm{x}+\frac{y^{2}}{x} \tag{8Marks}
\end{equation*}
$$

(b) Find the equation of the curve which passes through (1,2) and satisfies the following equation:

$$
\begin{equation*}
2 \mathrm{xy} \frac{d y}{d x}=\mathrm{x}^{2}+1 \tag{5Marks}
\end{equation*}
$$

(c) Determine the particular solution for the following equation:

$$
\begin{equation*}
\frac{d y}{d x}-\frac{y}{x-2}=(x-2)^{2} \quad \text { given } \mathrm{y}=8 \text { when } \mathrm{x}=2 \tag{7Marks}
\end{equation*}
$$

## QUESTION THREE

(a) Determine area bounded by the functions $y=x^{3}$ and $y=2$
(b) An area is bounded by the curve $y=\operatorname{Cos}^{2} x$, and lines $y=0$, and $x=\pi / 4$
(i) Calculate the area
(ii) Find volume for the solid of revolution to be generated if the area is rotated about x -axis through revolution.

## QUESTION FOUR

(a) Solve the equation;

$$
\begin{equation*}
\frac{d^{2} y}{d x^{2}}+2 \frac{d y}{d x}-6 y=3 \tag{7marks}
\end{equation*}
$$

(b) The motion of a vibrating body is defined by the following differential equation:

$$
\frac{d^{2} x}{d t^{2}}+3 \frac{d x}{d t}=5 \quad \text { where } \mathrm{x} \text { is the displacement in meters. }
$$

Solve the equation given that $\mathrm{t}=0, \mathrm{x}=0$ and $\frac{d x}{d t}=0$ and hence determine the velocity for the body at time $\mathrm{t}=4$ seconds.

## QUESTION FIVE

(a) Determine area bounded by the functions $y=4 x^{2}+1$ and $y=1$
(b) Figure 1 shows a T section of a beam. Use the section to determine the following:
(i) Second moment of area about $\mathrm{x} x^{\prime}$ axis.
(ii) Radius of gyration.


Fig. 1

