

FACULTY OF APPLIED AND HEALTH SCIENCES
DEPARTMENT OF MATHEMATICS AND PHYSICS
CERTIFICATE IN INFORMATION COMMUNICATION AND MAINTENANCE
AMA 1152 MATHEMATICS
END OF SEMESTER EXAMINATION
SERIES DECEMBER 2016
TIME 2 HOURS

INSTRUCTIONS TO CANDIDATES

This paper consists of five questions

Answer question one compulsory and any other two questions

Q1.

(a) i) Convert $2/11$ into decimal (2marks)

ii) Evaluate $5(3 \times 4^2 - 6 \div 7)$ (2marks)

iii) Rationalize

$$\frac{1}{1 + \sqrt{5}} \quad (2marks)$$

b) Add i) $11011_2 + 1011_2$ (2marks)

ii) $1110_2 + 1011_2$ (2marks)

iii) $1011_2 \times 111_2$ (2marks)

c) Solve

i) $x = \log_2 16$ (3marks)

ii) $\log x^4 - \log x^3 = \log 3x - \log 2x$ (3marks)

d) Given $A = \begin{pmatrix} 3 & 4 \\ 5 & 1 \end{pmatrix}$ and $B = \begin{pmatrix} 7 & 2 \\ 1 & 5 \end{pmatrix}$

Find i) AB (3marks)

ii) $3A - 5B$ (3marks)

e) Find the mean and mode of the following data

75, 70, 65, 67, 75, 74 (3marks)

f) Find the sum of the first 12 terms of the series $5 + 11 + 17 + \dots$

and the 20th term. (3marks)

Q2. Convert into decimal

i) 357.3_8 (3marks)

ii) 2AF3 hexadecimal to decimal (3marks)

b) Solve by quadratic formula $3x^2 + 4x + 1 = 0$ (3marks)

c) Given the series $a+ar+ar^2+\dots$ show that $S_n = a(1-r^n)/1-r$ (3marks)

d) Given  $A = 53^\circ$, $B = 61^\circ$ and $BC = 12.6$ cm

Find the unknown sides and angle. (3marks)

Q3.

a) Given $A = \begin{pmatrix} 7 & 3 \\ 2 & 5 \end{pmatrix}$

Find i) A^{-1} (3marks)

ii) A^T (2marks)

b) Solve by matrix method

$$3x+y=5$$

$$2x+7y=3 \quad (3marks)$$

c) Convert into radians

i) 150° (2marks)

ii) 120° (2marks)

d) Show that

i) $1+\tan^2 \theta = \sec^2 \theta$ (1mark)

ii) $\cos 2A = 2\cos^2 A - 1$ (2marks)

Q4.

a) Given the series $1 + \frac{1}{2} + \frac{1}{4} + \dots$

Find i) a_5 (1mark)

ii) s_{10} (2marks)

iii) s_{∞} (2marks)

b) Convert into Octal 492.731_{10} (3marks)

c) Convert into binary given 79_{10} (3marks)

d) A bag contains 5 red and 4 blue balls. Find the probability of picking with replacement, a red and a blue ball by use of a tree diagram. (4marks)

Q5.

a) Given $\cos A = \frac{2}{5}$ and that A is acute,

Find the other five trigonometric ratios. (5marks)

b) A is the event of throwing a six when a die is rolled and B is the event of drawing an ace from a pack of playing cards. Find the probability of the event both A and B. (2marks)

c) Solve by substitution

$$3x + 2y = 7$$

$$2x + 5y = 4 \quad (2marks)$$

d) If $\log 3 = 0.4771$ and $\log 2 = 0.3010$, write down

i) $\log 18$ (3marks)

ii) $\log 54$ (3marks)

In terms of $\log 2$ and $\log 3$ and hence evaluate.