TECHNICAL UNIVERSITY OF MOMBASA
FACULTY OF APPLIED AND HEALTH SCIENCES DEPARTMENT OF MATHEMATICS \& PHYSICS

UNIVERSITY EXAMINATION FOR: DIPLOMA IN MARINE ENGINEERING EMR 2106: ENGINEERING MATHEMATICS I END OF SEMESTER EXAMINATION SERIES: DECEMBER 2016<br>TIME: 2HOURS<br>DATE: Pick Date Dec 2016

## Instructions to Candidates

You should have the following for this examination
-Answer Booklet, examination pass and student ID
This paper consists of FIVE questions. Attempt question ONE (Compulsory) and any other TWO questions.
Do not write on the question paper.
Q. $1 \quad$ a) $\quad$ Obtain $7 / 15$ of $(15 \times 5 / 7)+(3 / 4 \div 15 / 16)$
(4 marks)
b) Copper, Zinc and another metal is used to form an alloy whose total mass is 96 Kg .

If Copper and Zinc form three quarters of the alloy, determine the mass of Zinc and copper in the alloy if their ratio is 5:1.
c) Solve for x in the equation.
(i) $\quad 1+2 \log _{3} \mathrm{X}=\log (28 \mathrm{x}-9$
(ii) $\frac{3^{o}}{9^{x^{2}}}=3^{x-1}$
d) Determine the smallest number of terms of the G.P.
$8+24+72+\ldots$. that will give a sum greater than $6,000,000$.
e) In an arithmetic progression, the sum of the first five terms is 30 , the third term is equal to the sum of the first two terms.

Determine the first five terms.
f) Write the following numbers in binary
$(246)_{8}$
(6 marks)
Q. 2 a) Convert the following numbers to binary numbers
(i) $\quad(21)_{10}$
(ii) $(543)_{8}$
(6 marks)
b) Convert the following to decimal number
(i) $(541)_{8}$
(ii) $(10101101)_{2}$
(iii) $\quad(\mathrm{a} 39)_{16}$
c) Convert to hexa-decimal
(i) $\quad(5071)_{10}$
Q. 3 a) The amount of money earned weekly by 40 people working as part-time in a factory, correct to the nearest 10 shs. Is as given;

| 80 | 90 | 70 | 110 | 90 | 160 | 110 | 80 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 140 | 30 | 90 | 50 | 100 | 110 | 60 | 100 |
| 80 | 90 | 110 | 80 | 100 | 90 | 120 | 70 |
| 130 | 170 | 80 | 120 | 100 | 110 | 40 | 110 |
| 50 | 100 | 110 | 90 | 100 | 70 | 110 | 80 |

Form a frequency distribution with 6 classes for these data.
b) The frequency distribution given below refers to the heights in centimeters of 100 people.

| Class | Frequency |
| :--- | :---: |
| $150-156$ | 5 |
| $157-163$ | 18 |
| $164-170$ | 20 |
| $171-177$ | 27 |
| $178-184$ | 22 |
| $185-191$ | 8 |

(i) Determine the mean height.
(ii) Determine the standard deviation.
c) The frequency distribution given below refers to the over-time worked by a group of craftsmen during each of 48 working weeks in a year.
(7 marks)

| Class | Frequency |
| :--- | :---: |
| $25-29$ | 5 |
| $30-34$ | 4 |
| $35-39$ | 7 |
| $40-44$ | 11 |
| $45-49$ | 12 |
| $50-54$ | 8 |
| $55-59$ | 1 |

Draw an ogive for this data and hence determine the quartile values.
Q. 4 a) The twenty first term of an AP is 37 and the sum of the first twenty terms is 320 .

Determine the sum of the first ten terms.
b) The third term of a G.P is 2 and the fifth is 18 .

Find the two possible values of the common ratio.
c) The sum to infinity of a GP with a positive common ratio is 9 and the sum of the first two terms is five.

Determine the first four terms of the progression.
d) Determine the number of terms of the AP.
$2+31 / 4+41 / 2+\ldots$ required to make a total of 204 .
Q. 5 a) Solve for $x$ in the equation.
(i) $\quad 9^{\mathrm{x}}+3^{2 \mathrm{x}-2}=30$
(ii) $\quad 2^{x-3}=3^{x-3.3691}$
(10 marks)
b) Solve for $x$ in the following equations
(i) $\log _{16} 4-\log _{4}(x+953)=-9 / 2$
(ii) $\quad \log _{x}^{3}+5 / 2 \log _{3} x=2$

