TECHNICAL UNIVERSITY OF MOMBASA

FACULTY OF APPLIED AND HEATH SCIENCES<br>MATHEMATICS DEPARTMENT<br>UNIVERSITY EXAMINATION FOR:<br>UPGRADING IN MATHEMATICS PPI<br>AMA 1004: COMMERCIAL ARITHMETICS AND STATISTICS.<br>END OF SEMESTER EXAMINATION<br>SERIES: DECEMBER 2016<br>TIME: TWO HOURS<br>DATE: DECEMBER 2016

## Instructions to Candidates

You should have the following for this examination
-Answer Booklet, examination pass and student ID
This paper consists of FIVE questions. Attempt Question ONE and any other TWO.
Do not write on the question paper.

## Question ONE

a) A Canadian tourist came to Kenya with sterling pounds 5000 which he exchanged to Kenyan shillings. He spent three quarters of the money and exchanged the rest to sterling pounds on leaving. How much to the nearest pound did he receive given the exchange rate? ( 4 mks )

Buying selling
$119.72 \quad 119.86$
b) A salesman earns a basic salary of Kshs. 19,000 per month. In addition, he earns a commission of 5\% for all sales above Ks. 20,000. In February 2011, he sold goods worth 115,000.

Calculate his total earnings that month.
( 3 marks )
c) A basket ball team play 10 matches in a tournament. The following are scores in each match.
$9,15,17,16,7,20,21,15,10,12$
Determine:
(a) the mode.
(b) the median.
d) The probability that a day is rainy is $1 / 4$. The probability that a teacher carries an umbrella on a rainy day is $1 / 7$ and that he carries an umbrella on a non-rainy day is ${ }^{2 /}{ }_{7}$. Find the probability that a teacher carries an umbrella. (3mks)
e) A man invests Ksh 10000 in an account which pays $16 \%$ interest p.a. The interest is compounded quarterly. Find the interest earned after $11 / 2$ years to the nearest shilling. (4mks)
f) Find the quartile deviation for the data below $235,418,626,405,335,717,504,609,414,431,918$. (3mks)
g) Using Cramer's Rule to solve for the unknowns in three linear equations: ( 5 mks )

$$
\begin{aligned}
& 5 x_{1}-2 x_{2}+3 x_{3}=16 \\
& 2 x_{1}+3 x_{2}-5 x_{3}=2 \\
& 4 x_{1}-5 x_{2}+6 x_{3}=7
\end{aligned}
$$

h) State all the integral values of $x$ that satisfy the following inequality.

## $2 x-3 \leq 3 x+5 \geq 7 x+6$

i) A wholesaler sold a cell phone to a retailer making a profit of $20 \%$. The retailer later sold the cell phone for Ksh. 3120 making a profit of $30 \%$ calculate the amount of money the wholesaler had paid for the cell phone. (3 marks)

## Question TWO

(a) The table below shows the marks scored by 40 students in a test.

| Marks | $10-19$ | $20-24$ | $25-29$ | $30-34$ | $35-39$ | $40-49$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Frequently | 3 | 4 | 7 | 10 | 9 | 7 |

(i) Calculate the mean mark.
(ii) Calculate the median mark.
(iii) Calculate the standard deviation.
b) Wambua invested Sh. 6400 at $15 \%$ per annum compound interest for 3 years. Muinde invested twice that amount at $12 \frac{1}{2} \%$ per annum simple interest for the same period of time. Find whose investment earned more interest and by how much.
c) Find the value of $x$ given that

$$
\left(\begin{array}{ll}
\mathbf{2 x}-\mathbf{1} & \mathbf{1} \\
\mathbf{x}^{\mathbf{2}} & \mathbf{1}
\end{array}\right) \text { is a singular matrix. }
$$

(3mks)
d) A car valued at Ksh.500,000 in January 2008. Each year, it value depreciates at $12 \%$ p.a. Find after how long would the value depreciate to Ksh.250,000(3 marks)

## Question THREE

a) A survey was conducted on 160 students to determine their eating preferences; some of the probabilities calculated from the results are shown in the tree diagram below:

a) Copy and complete the tree diagram. (2mks)
b) How many of the students in the survey were female. (2mks
c) One of the students is selected at random .Find the probability that the student selected.
i) A female vegetarian.
ii) A vegetarian.
iii) A non-vegetarian.
d) A trader bought 8 cows and 12 goats for a total of Ksh.294,000. If he had bought 1 more cows and 3 more goats he would have spend Ksh.337,500.
(i) Form two equations to represent the above information. (2 marks)
(ii) Use matrix method to determine the cost of a cow and that of a goat. (4 marks)
e) The trader sold the animals he had bought making a profit of $40 \%$ per cow and $45 \%$ per goat.
(i) Calculate the total amount of money he received. (2 marks)
(ii) Determine his profit in Kenya shillings.
(2 marks)

## Question FOUR

(a) Kamene has 20 acres of land. She intends to grow maize and beans. She requires sh. 2,000 to plant an acre of maize and sh. 4,000 for an acre of beans. Twice the area to be planted with maize should not be less than the one of beans. The total capital available is sh. 60,000 . The estimated profit is sh. 5,000 for an acre of maize and sh. 7,000 for an acre of beans. By letting x and y to represent the area to be planted with maize and beans respectively.
(i) Find the inequalities to represent the above information. (4 marks )
(ii) On the square grid provided, graph the above inequalities and show the region which satisfy them simultaneously. (Use the scale 3 cm rep. 5 units on both axes.) ( 4 marks)
(iii) Determine the expected maximum profit.
(b) Solve the inequalities $\chi \leq 2 \chi+7 \leq-\frac{1}{3} \chi+14$ hence represent the solution on a number line.
(c ) Use the inverse matrix method rule to solve simultaneous equations.

$$
\begin{align*}
& 2 \chi+y=10  \tag{3mks}\\
& 2 \chi+2 y=14
\end{align*}
$$

(d) Determine the quartile deviation of the set of numbers below.
$8,2,3,7,5,11,2,6,9,4$

## Question FIVE

(a) Mwaniki, Kamau and Kitheka started a joint Venture by contributing sh. 240,000, sh. 270,000 and sh. 300,000 respectively. They agreed that $30 \%$ of the profit made at the end of each year will be ploughed back into the business. They also agreed that $40 \%$ of the profits will cover salaries and other expenses for that year. The remainder was to be shared among the three partners in the ratio of their contributions. At the end of the first year, the business realized a gross profit of sh. 180,000.

Calculate how much each received at the end of the year.
b) Hellen's earnings are as follows:

Basic salary sh. 38000 per month
House allowance sh. 14000 per months
Travelling allowance sh. 8500 per month and Medical allowance Ksh. 3300 per month.
She is given a personal relief of Ksh. 12672
The table for payable tax is shown below

| Income in Ksh p.a | Payable tax $\%$ |
| :--- | :---: |
| $0-120000$ | 10 |
| $120001-240000$ | 15 |
| $240001-360000$ | 20 |
| $360001-480000$ | 25 |
| $480001-600000$ | 30 |
| $600001-720000$ | 35 |
| $720001-840000$ | 40 |
| $840001-960000$ | 45 |
| Over 960000 | 50 |
| late |  |

## Calculate

(a) (i) Hellen's taxable income in Ksh p.a
(ii) Her P.A.Y.E
(b) Hellen is deducted the following items per month

NHIF
Ksh. 320
Cooperative shares Ksh. 2000
Loan repayment Ksh5000
Determine her net salary per month
( c ) Using Cramer's Rule to solve for the unknowns in three linear equations: (5mks)

$$
\begin{aligned}
& 3 x_{1}+4 x_{2}-3 x_{3}=5 \\
& 3 x_{1}-2 x_{2}+4 x_{3}=7 \\
& 3 x_{1}+2 x_{2}-x_{3}=5
\end{aligned}
$$

