TECHNICAL UNIVERSITY OF MOMBASA

## FACULTY OF ENGINEERING AND TECHNOLOGY DEPARTMENT OF MEDICAL ENGINEERING <br> UNIVERSITY EXAMINATION FOR: <br> DIPLOMA IN MEDICAL ENGINEERING

## AMA2351:ENGINEERING MATHEMATICS VI

END OF SEMESTER EXAMINATION
SERIES:AUGUST2016
TIME:2HOURS
DATE:9Aug2016

## Instructions to Candidates

You should have the following for this examination
-Answer Booklet, examination pass and student ID
This paper consists of FIVE questions. Attemptquestion ONE (Compulsory) and any other TWO questions.
Do not write on the question paper.

## Question ONE

(a) Evaluate f (15), given the following table of values:

| $x$ | 10 | 20 | 30 | 40 | 50 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $f(x)$ | 46 | 66 | 81 | 93 | 101 |

(10 marks)
(b)
(i) Determine the Maclaurin series for the functions $e^{x}$ and $\sin x$ hence expand the $e^{\sin x}$ up to the term in fourth power
(ii) Using the series in (a) above evaluate $\int_{0}^{1} e^{\sin x} d x$
(10 marks)
(b) Evaluate the following
i) $\quad \int_{1}^{3} \int_{0}^{\ln y} d y d x$.
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ii) $\quad \int_{0}^{2} \int_{1}^{3} \int_{1}^{2} x y^{2} d z d y d x$
(10 marks)

## Question TWO

(a) Using Newton-Raphson iterative formula, determine the cube root of 123 correct to five decimal places
(b) Express $\sin (x+h)$ as a series of powers of $h$ hence evaluate $\sin 44^{\circ}$ correct to five decimal places
(10 marks)

## Question THREE

(a) Given the polynomial $x^{4}-x^{3}-2 x-34=0$ determine
i) the best approximation
ii) root of the equation correct to four significant figures taking $x_{o}=3$
(b) Using Newton's method determine the positive roots of the quadratic equation

$$
5 x^{2}+11 x-17=0 \text { correct to three significant figures }
$$

(10 marks)

## Question FOUR

(a) Determine the first four Taylor series terms for the following
i) $(x-1) e^{x}$
ii) $x^{2}+x-2$
(b) Determine the volume of the solid that lies below the surface given by $z=16 x y+200$ and lies above the region in the $x y$-plane bounded by $y=x^{2}$ and $y=8-x^{2}$.
(10 marks)

## Question FIVE

(a) Determine the Maclaurin series for the following.
(i) $\sin ^{2} x$
(ii) $\frac{x}{1-x^{2}}$
(b) Evaluate
(i) $\int_{0}^{1} \int_{3}^{2} \int_{1-y}^{y+2} 2 x y d x d y d z$
(ii) $\int_{0}^{\frac{\pi}{3}} \int_{0}^{2 a \cos \theta} r d r d \theta$ (10 marks)

