



# TECHNICAL UNIVERSITY OF MOMBASA

FACULTY OF ENGINEERING AND TECHNOLOGY

DEPARTMENT OF MEDICAL ENGINEERING

UNIVERSITY EXAMINATION FOR:

DIPLOMA IN MEDICAL ENGINEERING

AMA2351: ENGINEERING MATHEMATICS VI

END OF SEMESTER EXAMINATION

**SERIES: APRIL 2016**

**TIME: 2 HOURS**

**DATE: 9 May 2016**

## Instructions to Candidates

You should have the following for this examination

-Answer Booklet, examination pass and student ID

This paper consists of **FIVE** questions. Attempt question ONE (Compulsory) and any other TWO questions.

**Do not write on the question paper.**

## Question ONE

- a) Given that  $x_r$  is the approximation of the root to the equation  $x^4 + 5x - 20 = 0$ , determine
- the better approximation
  - roots of the equation taking  $x_0 = 1.8$  (10 marks)
- b) Determine the first four Taylor series terms for the following
- $(x - 1)e^{-x}$
  - $x^2 + x - 2$  (10 marks)
- c) Determine the Maclaurin series for  $\sin^2 x$  hence evaluate  $\int_0^{\pi} f(x) dx$  (10 marks)

## Question TWO

- a) Using Newton's method determine the positive roots of the quadratic equation
- $$5x^2 + 11x - 17 = 0 \text{ correct to three significant figures} \quad (10 \text{ marks})$$
- b) Determine a polynomial in  $x$  which takes on the values  $-3, 3, 11, 27, 57, 107$  when  $x = 0, 1, 2, 3, 4, 5$  respectively. (10 marks)

### Question THREE

Determine the Maclaurin series for the following

- a.  $\sin^2 x$
- b.  $\frac{x}{\sqrt{1-x^2}}$
- c.  $xe^{-x}$
- d.  $\frac{x}{1+x^2}$

(20 marks)

### Question FOUR

a) Expand  $\log_e \frac{1+x}{1-x}$  in power series hence evaluate  $\log_e 3$  correct to five decimal places (10 marks)

b) Use Newton-Raphson iterative method to solve  $x = 2 \sin x$  taking  $x_0 = 1.5$  (10 marks)

### Question FIVE

a) Given the data below use Newton-Gregory interpolation to evaluate

- i)  $f(0.36)$
- ii)  $f(0.44)$

x	0.2	0.3	0.4	0.5	0.6
y	0.234	0.2788	0.3222	0.3617	0.3979

(10 marks)

b) Determine Maclaurin expansion for  $e^x \ln(1+x)$  (10 marks)