



TECHNICAL UNIVERSITY OF MOMBASA

FACULTY OF APPLIED AND HEALTH SCIENCES
DEPARTMENT OF MATHEMATICS AND PHYSICS
UNIVERSITY EXAMINATION FOR:
BACHELOR OF SCIENCE IN COMMUNITY HEALTH /BSMR
AMA 4104 / AMA 4104: MATHEMATICS FOR SCIENCES
PAPER 11
END OF SEMESTER EXAMINATION
SERIES: FIRST SEMESTER YEAR ONE
TIME: 2 HOURS
DATE: APRIL 2016

Instructions to Candidates

You should have the following for this examination

-Answer Booklet, examination pass and student ID

This paper consists of FIVE Questions. Attempt **QUESTION ONE** and any other TWO.

Do not write on the question paper.

QUESTION ONE (30 MARKS)

- a) (i) Simplify $\frac{x^{\frac{2}{3}} \times y^{\frac{1}{3}}}{(x^4 y^2)^{\frac{1}{6}}}$ (4marks)
- (ii) Simplify $\sqrt{5+2\sqrt{6}}$ (6 marks)
- b) When the expression $px^4 + qx^3 + 3x^2 - 2x + 3$ is divided by $x^2 - 3x + 2$ the remainder is $x+1$; find the values of p and q . (6 marks)

- c) The roots equation $x^2 + 5x - 7 = 0$ are α, β . Find the equation whose roots are α^2 and β^2 without solving the quadratic equation. (5 marks)
- d) Two points A and B on a straight coastline are 1km apart B being due east of A. If a ship is observed on bearing 167° and 205° from A and B respectively. What is its distance from the coastline at A and B. (4 marks)
- e) A bag contains 3 black balls and 2 white balls. A ball is taken from the bag without being replaced ; a second ball is chosen. Using a tree diagram, find the probability that:
- They are both black
 - One is black and one is white. (5marks)

QUESTION TWO (20 MARKS)

- a) A drilling machine is to have 6 speeds ranging from 50 rev/min to 750 rev/min. If the speeds form a geometric progression, determine their values, each correct to the nearest whole number. (6 marks)
- b) Simplify $\frac{x^2(x^2 + 1)^{\frac{-1}{2}} - (x^2 + 1)^{\frac{1}{2}}}{x^2}$ (5 marks)
- c) The nth term in the series $2\frac{1}{2}, 4, 5\frac{1}{2}, 7, \dots$ is 22. find the number of terms. (4marks)
- d) Obtain the first four terms of the expansion of $(1 + \frac{1}{2}x)^{10}$ in ascending powers of x. Hence find the value of $(1.0005)^{10}$ correct to four decimal places. (5 marks)

QUESTION THREE (20 MARKS)

- a) By completing the square, find the greatest values of the function $f(x) = -7 + 12x - 3x^2$ (5 marks)
- b) (i) A radio tube may be purchased from five suppliers. In how many ways can three suppliers be chosen from the five. (2 marks)
- (ii) How many even numbers greater than 2000, can be formed with the digits 1,2,4,8, if each digit maybe used only once in each number. (5 marks)
- c) In a factory production process is known to be 5% defective. From a large batch of items produced by the process, two are selected at random. What is the probability that:
- Both will be good
 - Both will be defective
 - The first is good and the second is defective and
 - The first is defective and the second is good. (8marks)

QUESTION FOUR (20 MARKS)

- a) Draw the graph of $y = \sin 2\theta$ for values of θ from 0° to 360° at intervals of 30° (7 marks)
- b) The roots of the equation $x^2 + 6x + q = 0$ are α , and $\alpha - 1$. Find the value of q . (5 marks)
- c) Solve the following equations by methods indicated:
- (i) $5x^2 - 10x + 4 = 0$, giving your answer to three significant figures. (Quadratic formulae). (4 marks)
- (ii) $3x^2 + 8x - 3 = 0$ (completing the square) (4 marks)

QUESTION FIVE (20 MARKS)

- a) From the frequency distribution given below, find :
- (i) the mean using an assumed mean $A=27$ (4 marks)
- (ii) the mode. (5 marks)

| Height | frequency |
|---------|-----------|
| 10 – 14 | 12 |
| 15 – 19 | 17 |
| 20 – 24 | 22 |
| 25 – 29 | 27 |
| 30 – 34 | 32 |
| 35 – 39 | 37 |
| 40 – 44 | 42 |

- b) In a triangle XYZ, $YZ = 15.2$ cm, angle $YXZ = 51^\circ$ and $XYZ = 67^\circ$. Calculate :
- (i) The unknown sides and angle (5marks)
- (ii) The area of triangle XYZ (2 marks)
- c) Express $\log \frac{100a^2}{b^3 \sqrt{c}}$ in terms of $\log a$, $\log b$ and $\log c$ (4 marks)