TECHNICAL UNIVERSITY OF MOMBASA
FACULTY OF APPLIED AND HEALTH SCIENCES

# DEPARTMENT OF MATHEMATICS AND PHYSICS <br> UNIVERSITY EXAMINATION FOR: <br> BACHELOR OF SCIENCE IN COMMUNITY HEALTH / BSMR 

AMA 4104/AMA 4104: MATHEMATICS FOR SCIENCES

## PAPER 1

## END OF SEMESTER EXAMINATION <br> SERIES: FIRST SEMESTER YEAR ONE

TIME: 2 HOURS
DATE: APRIL 2016

## Instructions to Candidates

You should have the following for this examination
-Answer Booklet, examination pass and student ID
This paper consists of FIVE Questions. Attempt QUESTION ONE and any other TWO.
Do not write on the question paper.

## QUESTION ONE (30 MARKS)

a) (i) Simplify $\frac{\left(\frac{4}{3}\right)^{2} \times\left(\frac{3}{5}\right)^{-2}}{\left(\frac{2}{5}\right)^{-3}} \quad$ (4marks)
(ii) Evaluate

$$
\log 25-\log 125+\frac{1}{2} \log 625
$$

b) (i) Divide $4 a^{3}-6 a^{2} b+5 b^{3}$ by $2 a-b$ (4 marks)
(ii) Find the remainder when $x^{5}-4 x^{3}+2 x+3$ is divided by $\mathrm{x}-2$. (3marks)
c) Express $\frac{1}{1-\cos 45}$ in surd form and rationalize the denominator (4 marks)
d) Determine the nth term whose value is 22 in the series $2 \frac{1}{2}, 4,5 \frac{1}{2}, 7$. (4 marks)
e) The probability of a component failing in one year due to excessive temperature is $1 / 20$, due to excessive vibration is $1 / 25$ and due to excessive humidity is $1 / 50$; Determine the probabilities that during a one-year period a component;
(i) fails due to excessive temperature and vibration
(ii) fails due to excessive vibration and excessive humidity and
(iii) will not fail because of excessive temperature and excessive humidity
(7marks)

## QUESTION TWO (20 MARKS)

a) In an ecology field study the following frequency distribution was obtained on the height in centimeters of a certain plant species.

| Height $(\mathrm{cm})$ | $50-59$ | $60-69$ | $70-79$ | $80-89$ | $90-99$ | $100-109$ | $110-119$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| No. of <br> Plants | 7 | 81 | 192 | 312 | 218 | 82 | 18 |

Calculate the
(i) Mean height
(5 marks)
(ii) Median height
(5 marks)
b) Solve the following equations by the method indicated
(i) $6 x^{2}+x-2=0 \quad$ (factor method) (3 marks)
(ii) $2 x^{2}-1=3 x \quad$ (completing the square)
(4 marks)
c) How many committees can be formed from a group of 5 governors and 7 senators if each committee consists of 3 governors and 4 senators?
(3 marks)

## QUESTION THREE (20 MARKS)

a) The roots of the equation $2 x^{2}-7+4=0$ are $\alpha, \beta$. Find an equation with integral coefficients whose roots are $\alpha / \beta$ and $\beta / \alpha$
(7 marks)
b) Find by completing the square, the greatest value of the function $f(x)=1-6 x-x^{2}$
c) (i) Multiply and simplify $\cos x(\tan x-\sec x)$
(2marks)
(ii) Draw the graph of $\mathrm{y}=\cos \mathrm{x}$ for $-2 \pi<x<2 \pi$ and use the graph to solve for x if $\cos x=-0.5$

QUESTION FOUR (20 MARKS)
a) Evaluate the value of $\log _{2} 7$
(5 marks)
b) In a geometric progression, the sum of the second and third term is 9 , and the seventh term is eight times the fourth. Find:
(i) The first term
(2 marks)
(ii) common ratio
(5 marks)
(iii) Fifth term
(2marks)
c) Derive the quadratic formulae.

## QUESTION FIVE (20 MARKS)

a) Expand $\frac{1}{(4-x)^{2}}$ in ascending powers of $x$ as far as the term in $x^{3} \quad(7$ marks)
b) In a triangle $\mathrm{PQR}, \mathrm{PQ}=35 \mathrm{~cm}, \mathrm{QR}=45 \mathrm{~cm}$ and $\mathrm{PR}=65 \mathrm{~cm}$. Calculate :
(i) The size of angle PQR
(4marks)
(ii) The area of triangle PQR
(3 marks)
c) Solve the equation $3 e^{2 x}-7 e^{x}+2=0$
(6 marks)

