

TECHNICAL UNIVERSITY OF MOMBASA

INSTITUTE OF COMPUTING AND INFORMATICS

DEPARTMENT OF COMPUTER SCIENCE & INFORMATION TECHNOLOGY

UNIVERSITY EXAMINATION FOR:

BACHELOR OF BUSINESS & INFORMATION TECHNOLOGY/ BACHELOR

OF TECHNOLOGY IN INFORMATION TECHNOLOGY

EIT 4110: DISCRETE STRUCTURES

END OF SEMESTER EXAMINATION

SERIES:APRIL2016

TIME:2HOURS

DATE: Pick DateSelect MonthPick Year

Instructions to Candidates

You should have the following for this examination

-Answer Booklet, examination pass and student ID

This paper consists of **FIVE** questions. Attemptquestion ONE (Compulsory) and any other TWO questions.

Do not write on the question paper.

Question ONE

a) Define the following terms

(8 marks)

- i) A proposition
- ii) A predicate
- iii) Tautology
- iv) Contradiction

b) Compute the truth table for the statement

 $[(p \land q) \lor r] \Rightarrow (\tilde{q})$

(8 marks)

c) State and explain the Pigeonhole principle.

(4 marks)

- d) How many ways can a committee of three faculty members and two students be selected from seven faculty members and 8 students. Show your work. (6 marks)
- e) Translate the following proposition into a sentence in English

(4 marks)

Ouestion TWO

Differentiate between the following terms

(20 marks)

- a) Permutation and combination
- b) Random experiment and events
- c) Elementary events and compound events

- d) Mutually exclusive events and complementary events
- e) Open sentence and logical reasoning

Question THREE

a) Prove that the statement $\ (p \to q) \lor (q \to p) \ \ \mbox{is a tautology}.$ (6 marks)

b) Prove by mathematical induction that $1^2+2^2+3^2+\ldots+n^2=rac{n(n+1)(2n+1)}{6}$

(6 marks)

c) Given that A ={1,3,5,7,9, 11,13,17}, B= {5,9,13,17}

i) Find A – B (3 marks)

ii) Using Venn diagram to represent (i) above (3 marks)

iii) Show using a diagram that set B is a proper subset of set A. (2 marks)

Ouestion FOUR

- a) City residents were surveyed recently to determine readership of newspapers available. 50% of the residents read the morning paper, 60% read the evening paper, and 20% read both newspapers. Find the probability that a resident selected reads either the morning or evening paper or both the papers. (5 marks)
- b) There are three factories J, K, L supplying goods to warehouses A, B, C and D, the amount of supplies from the factories to warehouses are shown below.

Warehouses Factory	A	В	С	D	Total
J	72	16	15	50	153
K	38	18	13	22	91
L	50	32	22	43	147
Total	160	66	50	115	391

Find the following (9 marks)

 $J \cup A$

ii) C ∪ L

iii) ^{K∪D}

c) Write down a truth table to show that $\sim (p \lor q)$ is equivalent to $(\sim p) \land (\sim q)$ (6 marks)

Question FIVE

- a) A survey of 126 Kenyan students found that:
- 92 students are taking at least an English class
- 90 students are taking at least a Math class
- 68 students are taking at least a Science class
- 36 students are taking English, Math, and Science classes
- 68 students are taking at least English and Math classes
- 47 students are taking at least Math and Science classes
- 51 students are taking at least English and Science classes
 - i) Draw a Venn diagram to represent the above information. (4 marks)
 - ii) How many students are only taking an English class? (4 marks)
 - iii) How many are taking only Math and Science classes? (4 marks)
 - iv) How many students are not taking English, Math, or Science classes? (4 marks)

b) The table below specifies a Boolean function $f: S \times S \times S \longrightarrow S$

,,	ne below specifies a boolean function							
	Х	У	Z	f(x, y, z)				
	0	0	0	1				
	0	0	1	1				
	0	1	0	0				
	0	1	1	0				
	1	0	0	1				
	1	0	1	1				
	1	1	0	0				
	1	1	1	0				

Give a Boolean expression corresponding to this function.

(4 marks)