



TECHNICAL UNIVERSITY OF MOMBASA

FACULTY OF APPLIED AND HEALTH SCIENCE

DEPARTMENT OF MATHEMATICS AND PHYSICS

UNIVERSITY EXAMINATION FOR

**THE DEGREE OF BACHELOR OF TECHNOLOGY IN APPLIED PHYSICS,
RENEWABLE ENERGY AND ENVIRONMENTAL PHYSICS & BACHELOR SCIENCE
IN STATISTICS AND COMPUTER SCIENCE, MECHANICAL, CIVIL, ELECTRICAL
AND ELECTRONICS ENGINEERING**

SMA2278/ SMA 2271 / AMA 4204: ORDINARY DIFFERENTIAL EQUATIONS

END OF SEMESTER EXAMINATION- SERIES: MAY 2016

TIME: 2 HOURS

Instructions to Candidates

You should have the following to do this examination:

-Answer Booklet, examination pass and student ID

Do not write on the question paper.

Answer question One and any other two

Question ONE (30 marks)

- a) Using the differential operator evaluate $(D^2 + 5)\{\sin x\}$. (3 marks)
- b) Using a solution form the complimentary function of $y'' - y = e^x$ hence solve by reduction of order to obtain the particular integral. (6 marks)
- c) Use Bernoulli's method to solve $2x \frac{dy}{dx} - y = 4y^3$. (5 marks)

d) Find the inverse laplace transform of $F(S) = \frac{s+2}{s^2-4s+3}$ (4 marks)

e) Determine the general solution if $(x+y)dx + (3x+3y-4)dy = 0$ (6 marks)

f) The initial temperature of a body is 53°C and after 5 minutes its temperature is 45°C , from Newton's law of cooling it is known that the rate of cooling of a body is proportional to the temperature difference between the body and its surrounding room temperature. Use this to predict the temperature of the body after a further 5 minutes given that the room temperature was constant at 21°C . (6 marks)

Question TWO (20 marks)

a) Solve the linear fractional differential equation $\frac{dy}{dx} = \frac{x+y-3}{x-y-1}$. (7 marks)

b) Obtain the complimentary function hence find the particular integral of $(D^2 + 1)y = \tan x$ by variation of parameter method. (9 marks)

c) Solve the differential equation $\frac{d^2y}{dx^2} + 4\frac{dy}{dx} + 5y = 0$. (4 marks)

Question THREE (20 marks)

a) Identify all regular singular points in the differential equation

$(x^3 - 3x^2 + 2x)\frac{d^2y}{dx^2} + (x-2)\frac{dy}{dx} + 4x^2y = 0$. (5 marks)

b) Solve the differential equation $\frac{d^2y}{dx^2} + 5\frac{dy}{dx} = 3$. (4 marks)

c) Use D-operator method to find the general solution to $(D^2 + 3D - 4)y = \sin 2x$. (5 marks)

d) An object moves with simple harmonic motion on the x axis. Initially it is located at a distance 46 m away from the origin when $t=0$ and has velocity $v=15\text{ m/s}$ and decelerating at 100m/s^2 directed towards the origin O. find the equation of the position at any time t. (6 marks)

Question FOUR (20 marks)

a) Solve the differential equation $\frac{dy}{dx} = \frac{y^2 - 1}{x}$ (4 marks)

b) Solve the differential equation $\frac{d^2y}{dx^2} + 14\frac{dy}{dx} + 49y = 0$. (3 marks)

c) Solve the linear differential equation $(x^2 + 9)\frac{dy}{dx} + xy = 0$ if $y(0)=1$. (5 marks)

d) If $y_1 = e^{2x}$ is a solution of $y'' - 4y = 0$ find a 2nd independent solution of this differential equation. (8 marks)

Question Five (20 marks)

a) Verify whether it's an exact differential equation hence solve $(y^3 + 2x)dx + (3xy + 1)dy = 0$. (5 marks)

b) Use Laplace transform to solve $\frac{dx}{dt} - 2x = 4$ given at $t=0$ then $x=1$. (6 marks)

c) An electric circuit consists of an inductance of 0.1 henry a resistance of 20 ohms and a condenser of capacitance 25 microfarads. Find the charge q and the current i at any time t , given that the initial conditions are $q=0.05$ coulombs and $i = \frac{dq}{dt} = 0$ when $t=0$ if

$$L \frac{d^2q}{dt^2} + R \frac{dq}{dt} + \frac{q}{C} = E(t).$$

(9 marks)

THE END