TECHNICAL UNIVERSITY OF MOMBASA

# FACULTY OF ENGINEERING AND TECHNOLOGY <br> DEPARTMENT OF MEDICAL ENGINEERING <br> UNIVERSITY EXAMINATION FOR: <br> DIPLOMA IN MEDICAL ENGINEERING <br> AMA2351:ENGINEERING MATHEMATICS VI <br> END OF SEMESTER EXAMINATION <br> SERIES:APRIL2016 <br> TIME:2HOURS 

DATE:9May2016

## Instructions to Candidates

You should have the following for this examination
-Answer Booklet, examination pass and student ID
This paper consists of FIVE questions. Attemptquestion ONE (Compulsory) and any other TWO questions.
Do not write on the question paper.

## Question ONE

a) Given that $x_{r}$ is the approximation of the root to the equation $x^{4}+5 x-20=0$, determine
i. the better approximation
ii. roots of the equation taking $x_{o}=1.8$
b) Determine the first four Taylor series terms for the following
i. $\quad(x-1) e^{x}$
ii. $\quad x^{2}+x-2$
c) Determine the Maclaurin series for $\sin ^{2} x$ hence evaluate $\int_{0}^{\frac{\pi}{6}} f(x) d x$

## Question TWO

a) Using Newton's method determine the positive roots of the quadratic equation
$5 x^{2}+11 x-17=0$ correct to three significant figures
b) Determine a polynomial in x which takes on the values $-3,3,11,27,57,107$ when $x=0,1,2,3,4,5$ respectively.

## Question THREE

Determine the Maclaurin series for the following
a. $\sin ^{2} x$
b. $\frac{x}{\sqrt{1-x^{2}}}$
c. $x e^{-x}$
d. $\frac{x}{1+x^{2}}$

## Question FOUR

a) Expand $\log _{e} \frac{1+x}{1-x}$ in power series hence evaluate $\log _{e} 3$ correct to five decimal places (10 marks)
b) Use Newton-Raphson iterative method to solve $x=2 \sin x$ taking $x o=1.5$

## Question FIVE

a) Given the data below use Newton-Gregory interpolation to evaluate
i) $f(0.36)$
ii) $f(0.44)$

| x | 0.2 | 0.3 | 0.4 | 0.5 | 0.6 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| y | 0.234 | 0.2788 | 0.3222 | 0.3617 | 0.3979 |

b) Determine Maclaurin expansion for $e^{x} \ln (1+x)$

