



# TECHNICAL UNIVERSITY OF MOMBASA

FACULTY OF HEALTH AND APPLIED SCIENCES

DEPARTMENT OF MATHS & PHYSICS

## UNIVERSITY EXAMINATION FOR:

DIPLOMA IN ELECTRICAL & ELECTRONIC ENGINEERING

DIPLOMA IN MECHANICAL ENGINEERING

AMA2151 ENGINEERING MATHEMATICS 2

## END OF SEMESTER EXAMINATION

**SERIES:** APRIL / MAY 2016 SERIES

**TIME:** 2HRS

**DATE:** APRIL / MAY 2016

### Instructions to Candidates

You should have the following for this examination

-Answer Booklet, examination pass and student ID Mathematical table, calculator, no mobile phone

This paper consists of **FIVE** questions. Attempt question ONE (Compulsory) and any other TWO questions.

**Do not write on the question paper.**

### QUESTION ONE

a) (i) Differentiate from first principles  $f(t) = kt^4$  (3 Mks)

(ii) Given  $x^3 + Y^3 - 3axy$  find  $\frac{dy}{dx}$  (2Mks)

(iii) Find the gradient at the point (1, 1) on the curve  

$$Y = \frac{(x^3 + 4x + 1)}{(x^2 + 2x + 3)}$$
 (4 Mks)

b) (i) If  $f(x) = 4x^3 - 2x^2 - 3x + 1$  find  

$$\frac{f(1+b) - f(1)}{b}$$
 (3Mks)

(ii) If box with sides of length x, y, z mm is expanding along the x and y sides at a rate of 2 and 3 mm per second but contracting along the z side at a rate of 4mm per second. Find the rate of change of volume when x=y=10mm, z=20mm (4 Mks)

(iii) If  $S = a \sin wt$  where a and w are constants prove that

$$\frac{ds}{dt} = \pm w\sqrt{a^2 - s^2} \quad \frac{d^2s}{dt^2} = -w^2s \quad (4Mks)$$

c) (i) Evaluate

$$I = \int (2x^3 - 5x^2 + 6x - 9) dx \quad (2Mks)$$

(ii) Determine  $\int_0^{\frac{\pi}{2}} (\sin x - \cos x) dx$  (2Mks)

(iii) Sketch the graph  $y = x^3 + 2x^2 + x + 1$  between  $x = -1$  and  $x = 2$  and determine the area enclosed between the curve, the x-axis and between the  $x = -1$  and  $x = 2$  (4Mks)

d) Find the mean value of  $y = 3x^2 + 4x + 1$  between  $x = -1$  and  $x = 2$  (2Mks)

### QUESTION TWO

a) Find (i)  $\lim_{n \rightarrow \infty} \frac{3n^2 - 7n - 10000}{2n^2 + n - 4}$  (3Mks)

(ii) Show that  $\lim_{x \rightarrow \infty} \frac{3x}{2x+1} = \frac{3}{2}$  (3Mks)

(iii) Evaluate:  $\lim_{x \rightarrow \infty} \frac{2+x}{3-7x}$  (3Mks)

b) (i) Determine algebraically, from first principles the gradient of the graph of  $y = 5x^2 + 2$  at the point p where  $x = -1.6$  (4Mks)

(ii) Investigate the stationary points on the graph of  $y = x^2 e^{-x}$  and sketch the curve (7Mks)

### QUESTION THREE

a) (I) Given that  $h(x) = x^2 - x$  find the values of

(i)  $h(10)$  (2Mks)

(ii)  $h(t+1)$  (2Mks)

(iii)  $h(5k)$  (2Mks)

(II) If  $f(x) = 7x$  and  $g(x) = x+3$  and  $fg : x \rightarrow y$  express as simply as possible the rule which maps  $x$  onto  $y$ . Find the values of  $p, q, r$  such that

- i)  $fg : 5 \rightarrow p$  (2Mks)
- ii)  $fg : 10 \rightarrow q$  (2Mks)
- iii)  $fg : r \rightarrow 35$  (2Mks)

b) (i) prove the identity  $\cosh^2 x - \sinh^2 x = 1$  from the definition (3Mks)

(ii) Prove that  $\sinh^{-1} x = \text{Ln}\{x + \sqrt{(1+x^2)}\}$  (3Mks)

#### **QUESTION FOUR**

a) (i) Find  $\int \frac{1}{\sqrt{(x^2+2x+10)}} dx$  by completing the square and substitution of

$$x+1 = 3\sin \theta. \quad (4Mks)$$

(ii) Find  $I = \int \sqrt{(a^2-x^2)} dx$  by putting  $x = a \sin \theta$  (4Mks)

b) (i) Integrate  $\frac{1}{(x+1)^2(x+4)}$  (6 mks)

(ii) Find  $I = \int x \sin x dx$  (3Mks)

(iii) If  $\tanh x = 1/3$  what is  $\text{sech} x$ ? (3Mks)

#### **QUESTION FIVE**

a) Evaluate

(i)  $I = \int_1^2 \int_0^{\pi} \int_0^{\pi} (3 + \sin \theta) d\theta dr$  (3Mks)

(ii)  $I = \int_1^2 \int_0^3 \int_0^1 (p^2+q^2-r^2) dpdqdr$  (4Mks)

b) Show that

(i)  $V = (Ar^n + B/r^n) \cos(n\theta - \alpha)$   
Satisfies the equation

$$\frac{d^2v}{dr^2} + \frac{1}{r} \frac{dv}{dr} + \frac{1}{r^3} \frac{d^2v}{d\theta^2} = 0 \quad (6Mks)$$

(ii) If  $z = \sin(x+y)$  where  $x = \mu^2 + v^2$  and  $y = 2\mu v$  find

$$\frac{dz}{d\mu} \text{ and } \frac{dz}{dv} \quad (7Mks)$$