# TECHNICAL UNIVERSITY OF MOMBASA <br> Faculty of Business and Social Studies 

DEPARTMENT OF BUSINESS STUDIES

## UNIVERSITY EXAMINATIONS FOR DEGREE IN BACHELOR OF BUSINESS ADMINISTRATION BACHELOR OF COMMERCE

## BMS 4102: MANAGEMENT ACCOUNTING II

END OF SEMESTER EXAMINATIONS
SERIES: APRIL 2015
TIME: 2 HOURS

## INSTRUCTIONS:

- Answer Question ONE (Compulsory) and any other TWO questions.
- Do not write on the question paper

This paper consists of Five printed pages

## QUESTION 1 (Compulsory)

a) Find the determinant of the following matrices:
i) $T=\left[\begin{array}{cc}8 & 3 \\ -2 & -4\end{array}\right]$
(2 marks)
ii) $A=\left[\begin{array}{ccc}2 & 4 & 7 \\ -1 & 3 & 2 \\ 4 & -2 & 0\end{array}\right]$
b) Differentiate the following functions;
i) $Y=\frac{2}{\left(2 t^{3}-5\right)^{4}}$
ii) $Y=3 x^{2} \sin 2 x$
c) Minimize $Z=3 x_{1}+6 x_{2}$ Subject to:

$$
\begin{aligned}
& 4 x_{1}+x_{2} \geq 20 \\
& x_{1}+x_{2} \leq 20 \\
& x_{1}+x_{2} \geq 10 \\
& x 1, x 2 \geq 0
\end{aligned}
$$

d) Solve for x and y by use of Cramer's rule
i) $\begin{aligned} & 5 x+3 y=1 \\ & 2 x-3 y=-8\end{aligned}$
ii) $\begin{aligned} & 24 x+2 y=86 \\ & 15 x+y=52\end{aligned}$
(3 marks)
e) Determine the inverse of the following matrix:
i) $\quad A=\left(\begin{array}{cc}4 & 3 \\ -2 & -1\end{array}\right)$
ii) $\quad B=\left[\begin{array}{ccc}1 & 2 & 0 \\ 1 & 0 & -1 \\ -1 & 3 & 2\end{array}\right]$
f) Integrate the following functions:
i) $\int 3 x^{4} d x$
ii) $\int \frac{2}{x^{2}} d x$

## QUESTION 2

a) Consider the system of equations and solve using matrices:

$$
\begin{aligned}
& x_{1}+2 x_{2}=5 \\
& x_{1}-x_{3}=-15 \\
& -x_{1}+3 x_{2}+2 x_{3}=40
\end{aligned}
$$

b) Differentiate the following functions:
i) $\left(3 x^{2}-5 x+8\right)^{10}$
ii) $x^{2} e^{2 x}$
c) Differentiate the following functions:
i) $Y=2 x^{2}(5 x+3)$
ii) $e^{3 t} \sin 4 t$
iii) $Y=\operatorname{Ln}\left(5 x^{2}-2 x+1\right)$

## QUESTION 3

a) Determine solution to the system of equations:

$$
\text { i) } \begin{align*}
& 3 x_{1}-5 x_{2}=22  \tag{3marks}\\
& 4 x_{1}+2 x_{2}=12 \\
& \text { ii) }  \tag{3marks}\\
& 2 x_{1}+3 x_{2}=1 \\
& 4 x_{1}+7 x_{2}=3
\end{align*}
$$

b) Intergrate the function
i) $Y=\int\left(12 x+24 x^{2}\right) d x$
ii) $Y=\int\left(48 x-0.4 x^{-1.4}\right) d x$
c) Find the determinant for each of the following matrices
i) $\left[\begin{array}{cc}-6 & 25 \\ -10 & -20\end{array}\right]$
(1 mark)
ii) $\left[\begin{array}{ccc}2 & 0 & -1 \\ 5 & 2 & 3 \\ -10 & 0 & 5\end{array}\right]$
d) Differentiate with respect to $x$
i) $y=2 \cos 6 x$
ii) $y=\frac{x^{2}}{1+x}$
(3 marks)
e) A producer of machinery wishes to maximize profit from producing two products, product A and product $B$. The three major inputs for each product are steel, electricity and labour hours. The table below summarizes the requirements per unit of each product, available resources and profit margin per unit. The number of units of product A should be no more than $80 \%$ of the number of product $B$. Formulate the linear programming model for this situation.

|  | Product |  |  |
| :--- | :--- | :--- | :--- |
|  | A | B | Monthly total available |
| Energy | 100 K wh | 200 K wh | $20,000 \mathrm{k}$ wh |
| Steel | 60 lb | 80 Lb | $10,000 \mathrm{Lb}$ |
| Labor | 2.5 h | 2 h | 400 h |
| Profit per unit | $\$ 30$ | $\$ 40$ |  |

## QUESTION 4

a) Solve the following simultaneous equations using Cramer's rule:
i) $\begin{aligned} & x_{1}+x_{2}=-1 \\ & 2 x_{1}-x_{2}=7\end{aligned}$
ii) $\begin{aligned} & 5 x_{1}-2 x_{2}=3 \\ & 3 x_{1}+x_{2}=-1\end{aligned}$
b) Differentiate the following functions:
i) $Y=\frac{x+1}{\sqrt{x}}$
ii) $Y=\left(3 x^{2}-7 x+4\right)^{6}$
iii) $Y=10 e^{5 x^{2}-4 x}$
c) Minimize $Z=5 x_{1}+8 x_{2}$

Subject to:

$$
\begin{aligned}
& x_{1}+x_{2} \geq 6 \\
& 3 x_{1}+2 x_{2} \leq 30 \\
& 2 x_{1}+x_{2} \leq 5 \\
& x_{1}, x_{2} \geq 0
\end{aligned}
$$

## QUESTION 5

a) Differentiate the following functions:
i) $Y=\frac{5}{3 \sqrt{x^{4}}}$
(3 marks)
ii) $Y=e^{x}$
(2 marks)
b) The population of a country is estimated by the function $P=125 e^{0.035 t}$ where P is equals the population (in millions) and t equals time measured in years since 1990.
i) What is the population expected to equal to in the year 2000.
ii) Determine the expression for the instantaneous rate of change in the population.
c) Solve the following linear programming problem

Maximize $z=2 x_{1}+10 x_{2}$
Subject to:

$$
\begin{aligned}
& 2 x_{1}+5 x_{2} \leq 16 \\
& 6 x_{1}+10 x_{2} \leq 30 \\
& x_{1} \geq 0, x_{2} \geq 0
\end{aligned}
$$

d) Differentiate the following function
$Y=3 x^{3}-2 x^{2}+x-4$
e) Give FOUR applications of linear programming.

