

# TECHNICAL UNIVERSITY OF MOMBASA <br> Faculty of Business \& Social Studies 

DEPARTMENT OF BUSINESS STUDIES

UNIVERSITY EXAMINATIONS FOR
MASTERS IN BUSINESS ADMINISTRATION

## BMS 5202: QUANTITATIVE TECHNIQUES

END OF SEMESTER EXAMINATIONS<br>SERIES: APRIL 2015<br>TIME: 3 HOURS

## INSTRUCTIONS:

- Attempt question ONE (Compulsory) and any other THREE questions
- Do not write on the question paper.

This paper consists of Five printed pages

## QUESTION 1 (Compulsory)

a) Distinguish between the following:
i) QT and management
ii) Solving the model and validating the model.
b) Given the following matrices:

$$
A=\left(\begin{array}{ll}
4 & 0 \\
0 & 7 \\
6 & 1
\end{array}\right) \quad B=\left(\begin{array}{ll}
4 & 6 \\
2 & 7 \\
6 & 1
\end{array}\right) \quad C=\left(\begin{array}{lll}
4 & 2 & 6 \\
1 & 8 & 7
\end{array}\right)
$$

Find
i) A.B
ii) $C^{T}$
iii) $\quad$ C. $C^{T}$
iv) B.C
v) C.B
(10 marks)
c) Find the inverse of $\left(\begin{array}{ccc}1 & 5 & -2 \\ 3 & -1 & 4 \\ -3 & 6 & -7\end{array}\right)$
d) Solve the following system of linear equation

$$
\begin{aligned}
& 2 x_{1}-4 x_{2}+5 x_{3}=36 \\
& -3 x_{1}+3 x_{2}-7 x_{3}=-7 \\
& 5 x_{1}+3 x_{2}-8 x_{3}=-31
\end{aligned}
$$

(6 marks)

## QUESTION 2

The table below summarizes the production of livestock and livestock products in UK.

Livestock and Livestock Products, Great Britain

|  |  | Type | 1981 | 1990 | 1991 |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Bacon and ham ('000 tons) | Product | 203 | 180 | 16 | 167 |
| Beef and veal ('000 tons) | Product | 1,021 | 997 | 1,023 | 970 |
| Cattle and calves ('000 head) | Livestock | 13,224 | 12,059 | 11,866 | 11,788 |
| Eggs (million dozen) ${ }^{* *}$ | Product | 1,024 | 811 | 822 | 812 |
| Milk (million litres) | Product | 15,973 | 14,535 | 14,075 | 13,995 |
| Mutton and lamb ('000 tons) | Product | 282 | 393 | 418 | 392 |
| Pigs ('000s head) | Livestock | 8,008 | 7,449 | 7,596 | 7,608 |
| Pork ('000 tons) | Product | 744 | 749 | 797 | 805 |
| Poultry ('000 head) | Livestock | 80,297 | 92,341 | 94,644 | 91,963 |
| Poultry meat ('000 tons) | Product | 788 | 1,027 | 1,074 | 1,069 |
| Sheep and lambs ('000 head) | Livestock | 33,078 | 43,799 | 43,621 | 43,973 |

## Required:

a) Work a report summarizing the major features of data. Include any relevant statistics, tables and graphs.
b) Describe any other information that you would require.

## QUESTION 3

The table below shows a sample of 14 families selected at random; length of banking days ( x ) in a hotel and cost of holiday $£(\mathrm{y})$.

| Customer name | Length of banking <br> days (x) | Cost of holiday £ (y) |
| :--- | :--- | :--- |
| Smith | 331 | 2115 |
| John | 52 | 1752 |
| Peter | 125 | 2044 |
| King | 270 | 2443 |
| Light | 5 | 1257 |
| Duff | 7 | 1490 |
| Stark | 207 | 2187 |
| Jane | 15 | 1545 |
| Caroline | 27 | 1560 |
| David | 183 | 1981 |
| Caroline | 36 | 1762 |
| Sara | 85 | 1875 |
| Jane | 22 | 1624 |
| Mary | 41 | 1728 |

The following summary statistics have been included:
$\Sigma x=1406$
$\Sigma y=25,363$
$\Sigma(x-x)=147,639.4$
$\Sigma(x-x))(y-y)=385,734.1$
$\Sigma(y-y)=1,311,949.2$
$\Sigma x^{2}=288,842$
$\Sigma y^{2}=47,260,647$
$\Sigma x y=2,932,904$

## Required:

a) Analyze the relationship between the length of the banking and the cost for the 14 families using regression analysis.
b) What would you expect the cost of the holiday to be if you booked:
i) 290 days in advance
ii) 180 days in advance
iii) 3 days in advance
c) Write a report on the analysis of the data. Indicate any additional information you would require and include any recommendation for further analysis.

## QUESTION 4

A car magazine has tested the acceleration (going from 0 to 60 miles per hour) of three sports cars. Each car was tested six times (in seconds)

| Car 1 | 6.17 | 7.00 | 6.69 | 6.03 | 5.87 | 6.82 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Car 2 | 7.10 | 6.17 | 6.90 | 6.54 | 6.41 | 5.94 |
| Car 3 | 5.88 | 6.89 | 6.32 | 6.49 | 6.34 | 5.82 |

a) Carry out one-way ANOVA.
b) Test whether there is a significant difference in the average acceleration time for the three cars.
(6 marks)
c) Write a report on your findings. Indicate any other information you would require. Detail your recommendations for further research and analysis.
(8 marks)

## QUESTION 5

The following table depicts time taken to relieve headache tested on 20 patients

## Time Taken to relieve a headache (minutes)

| 30.5 | 29.1 | 20.9 | 33.7 | 28.4 | 34.7 | 37.5 | 22.8 | 18.2 | 30.7 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 16.8 | 34.1 | 36.4 | 25 | 18.2 | 27.2 | 25.9 | 32.8 | 31.9 | 30.2 |

## Required:

a) Carry out an appropriate hypothesis test to determine the average time taken to relieve a headache with the new product is significantly different from the average taken by the established brand. Justify your answer.
(10 marks)
b) Carry out an appropriate hypothesis test to determine whether the average time taken to relieve a headache with the new product is significantly longer than the average time taken by the established brand. Justify your answer.
(6 marks)
c) Write a report on your findings. Describe any assumptions you have made. Indicate any further information you would require and any further analysis you would wish to perform.
(9 marks)

## QUESTION 6

Balph frequently ignores Dr. Rasp's excellent advice, and does not get a good night's sleep before attending a "knowledge festival'. Balph sets about to prove that he is right and Dr. Rasp is wrong. He surveys a random sample of 42 fellow-students, and obtains data on their grade point average and the number of times this semester which they have pulled and all-nighter. He fits a regression model to the data. The Microsoft. Excel output is given below. Also given are the mean and the standard deviation of the two variables.

| Regression Statistics |  |
| :--- | :---: |
| Multiple R | 0.546 |
| R Square | 0.298 |
| Adjusted R. Square | 0.281 |
| Standard Error | 0.997 |
| Observations | 42 |


|  | Mean | St. Dev. |
| :--- | :--- | :--- |
| AllNighters | 4.71 | 3.24 |
| GPA | 1.92 | 1.18 |

ANOVA

|  | $d f$ | $S S$ | $M S$ | $F$ | Significance $F$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Regression | 1 | 16.920 | 16.920 | 17.011 | 0.000 |
| Residual | 40 | 39.788 | 0.995 |  |  |
| Total | 41 | 56.708 |  |  |  |
|  |  |  |  |  |  |
|  | Coefficients | Standard | t Stat | P-value | Lower 95\% |
|  |  | Error |  |  |  |
| Intercept | 2.854 | 0.274 | 10.417 | 0.000 | 2.300 |
| AllNighters | -0.198 | 0.048 | -4.124 | 0.000 | -0.296 |

## Required:

a) Balph has 10 all-nights this semester. Predict his grade point average.
(4 marks)
b) Given an $80 \%$ interval for your results in Part (a).
(11 marks)
c) Do Balph's results tend to support Balph's or Dr. Rasp's point of view? Explain. Are the findings statistically significant?
d) One number in the printout ( 0.048 ) is shaded. Show how that number was computed.

