# TECHNICAL UNIVERSITY OF MOMBASA 

# FACULTY OF APPLIED AND HEALTH SCIENCES 

DEPARTMENT OF MATHEMATICS \& PHYSICS
UNIVERSITY EXAMINATION FOR:

## BACHELOR OF TECHNOLOGY AND RENEWABLEL ENERGY \& BACHELOR OF TECHNOLOGY AND APPLIED PHYSICS

## AMA 4109: CALCULUS FOR TECHNOLOGISTS 1 : <br> END OF SEMESTER EXAMINATION <br> SERIES:APRIL2016 <br> TIME:2HOURS

DATE:Pick DateMay2016

## Instructions to Candidates

You should have the following for this examination
-Answer Booklet, examination pass and student ID
This paper consists of FIVE questions. Attempt question ONE (Compulsory) and any other TWO questions.
Do not write on the question paper.

QUESTION ONE (COMPULSORY 30MKS)
a) Find the derivative of the following
i). $y=\sin ^{2} x$

$$
y=\tanh ^{-1} x
$$

ii)

$$
y=\operatorname{Cot}(\tan x)
$$

iii).
b). Show that $\tanh ^{2} x+\sec h^{2} x=1$
(3marks).
(4 marks)
c). A rectangular sheet of metal of length 6 meters and width 2 meters is given. Four equal
squares of sides $x$ meters are removed from the corners. The sides of this sheet are now turned up to form an open rectangular box. Find appropriately the height of the box which will give the maximum volume of the box.
d).Evaluate the following limits
i) $\quad \lim _{x \rightarrow 2} \frac{x^{2}-5 x+6}{x-2}$
(4 Marks)
ii) $\quad \operatorname{Lim}_{x \rightarrow 49} \frac{x-49}{6-\sqrt{x-13}}$

## QUESTION TWO (20MKS)

a).Given a parametric function $x=1-t^{2}, y=t^{2}-t$. Determine $\frac{d y}{d x}$ at $\mathrm{t}=2$. (4marks).
b). Find the turning points on the curve of $y=x^{3}-6 x^{2}+9 x-2$ and distinguish between them.
c). Determine the asymptotes to the curve $\quad y=\frac{(x-1)(x+6)}{(x+3)(x-4)}$.

## QUESTION THREE ( 20MKS)

a).If $y^{2}+x^{2}=2 y \sqrt{\left(1+x^{2}\right)}$ show that $\frac{d y}{d x}=\frac{x}{\sqrt{\left(1+x^{2}\right)}}$,
(5marks)
b).Determine the area enclosed by the functions $y=x^{3}+2 x^{2}-5 x-6, x=-3, x=2$ and the x -axis
c). By use of the product rule, determine $\frac{d^{2} y}{d x^{2}}$ of $y=x^{2} \sin 2 x$

QUESTION FOUR ( 20MKS)
a).Determine the equation of the normal to the curve $x^{2} y+y^{2} x-x^{3}+y^{2}=9$ at $(1,2)$ (6marks)
b).Evaluate

$$
\begin{align*}
& \text { (i). } \lim _{x \rightarrow 0} \frac{1-\sqrt{(1-x)}}{x}  \tag{4marks}\\
& \text { (ii) } \lim _{x \rightarrow 0} \frac{5+x}{x^{2}+x+1}
\end{align*}
$$

(3marks)
c). Differentiate $y=\cos x$ from first principals
(7marks

## QUESTION FIVE ( 20MKS)

a).Define continuity.
b). Gas is escaping from a spherical balloon at a rate of $0.01 \mathrm{~m}^{3} / \mathrm{s}$. How first is the radius changing when the surface area is $10 \mathrm{~m}^{2}$.
c). Prove that $\frac{d}{d x}\left(\frac{1+\sin x+\cos x}{1-\sin x+\cos x}\right)=\frac{1}{1-\sin x}$
(5marks
d).Determine

$$
\lim _{x \rightarrow \infty} \frac{\tan x-x}{x^{3}}
$$

