## TECHNICAL UNIVERSITY OF MOMBASA

## FACULTY OF APPLIED AND HEALTH SCIENCES

DEPARTMENT OF MATHEMATICS \& PHYSICS

## UNIVERSITY EXAMINATION FOR:

## BACHELOR OF TECHNOLOGY AND RENEWABLEL ENERGY \& BACHELOR OF TECHNOLOGY AND APPLIED PHYSICS

## AMA 4109: CALCULUS FOR TECHNOLOGISTS 1

## END OF SEMESTER EXAMINATION <br> SERIES:APRIL 2016 <br> TIME:2HOURS <br> DATE:Pick DateMay2016

## Instructions to Candidates

You should have the following for this examination
-Answer Booklet, examination pass and student ID
This paper consists of FIVE questions. Attempt question ONE (Compulsory) and any other TWO questions.
Do not write on the question paper.

## QUESTION ONE (COMPULSORY 30MKS)

a) Find the derivative of $y=2 x^{3}+3$ by the first principles
b).Find $\frac{d y}{d x}$ if $y^{2}=x^{2}+\sin x y$ (6 marks)
c). Evaluate the following limits

$$
\begin{equation*}
\text { i) } \quad \lim _{x \rightarrow o} \frac{\sqrt{x+3}-\sqrt{3}}{x} \tag{4marks}
\end{equation*}
$$

$$
\begin{equation*}
\text { ii) } \quad \lim _{x \rightarrow-2} \frac{x+2}{x^{2}+x-2} \tag{3Marks}
\end{equation*}
$$

d). Find the first derivative of the following function

$$
\begin{equation*}
y=\cos 3 x \ln x \tag{3marks}
\end{equation*}
$$

e).Determine the co-ordinates of the maximum and minimum values of the graph
$y=\frac{x^{3}}{3}+\frac{x^{2}}{2}-6 x+\frac{5}{3}$ and distinguish between them. Sketch the graph.

## QUESTION TWO ( 20MKS)

a).An object at the end of a vertical spring is stretched 4 cm beyond its rest position and released to move in simple harmonic motion from $\mathrm{t}=0$. Its position at time t is $S=f(t)=4 \operatorname{cost}$. Find its velocity and acceleration.
b).Define $f(2)$ in a way that extends $f(x)=\frac{x^{2}+x-6}{x^{2}-4}$ to be continuous at $x=2$
c). $\lim _{x \rightarrow 1} \frac{x^{3}-1}{x-1}$. Evaluate
d).Differentiate $\quad y=x^{2} \tan x$
e). Determine the asymptotes to the curve $\quad y=\frac{(x-1)(x+4)}{(x-2)(x-3)}$
(3 Marks).
(7marks)

## QUESTION THREE ( 20MKS)

a) Find $\frac{d y}{d x}$ in the following
i) $y=\sqrt{3 x^{2}+4 x-1}$
(3 marks)
ii) $\quad x^{3} \sec (x y)=\ln y$
(4 marks)
iii). $x^{2} y=e^{\sin 5 x}$
(4marks)
iv). $y=\log _{e}\left(x^{2}-6 x+8\right)$, at $x=1$
b). Determine the area of the largest piece of rectangular ground that can be enclosed by 100 m of fencing, if part of the existing straight wall is used as one side
(5 marks).

## QUESTION FOUR ( 20MKS)

a). Find the equation of the tangent to the curve given by $y=t^{3}+1$ and $x=t+2$ at the point $(1,0)$ (6 marks)
b). Using first principle, Show that $\frac{d(\sin x)}{d x}=\cos x$ (6 marks)
c).Find $\frac{d y}{d x}$ for the following functions

$$
\text { i) } \quad y=\left(3 x^{2}-\sin 2 x\right)^{2}
$$

ii) $y=\sqrt{\ln e^{2 x}}$
(4 marks)

## QUESTION FIVE ( 20MKS)

a) Find $\frac{d^{2} y}{d x^{2}}$ for the following

$$
\begin{equation*}
x=t^{3}, y=3 t^{2}+5 \tag{4Marks}
\end{equation*}
$$

b) A projectile is fired straight upwards with a velocity of $400 \mathrm{~m} / \mathrm{s}$. its distance above the ground $\mathrm{t}-$ seconds after being fired is given by $S(t)=-16 t^{2}+400 t$. Find
(i) The time after which the projectile hits the ground.
(ii) The velocity at which the projectile hits the ground
(iii) The maximum altitude achieved by the projectile
(4 Marks)
(iv) The acceleration at any time t
c). A ladder 20 m long is leaned against a vertical wall. If the bottom of the ladder slides away from the wall at the rate of $2 \mathrm{~m} / \mathrm{s}$. How fast is the ladder sliding down when the top of the ladder is 12 m above the ground?
(5marks)

