



# TECHNICAL UNIVERSITY OF MOMBASA

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FACULTY OF APPLIED & HEALTH SCIENCES

MATHEMATICS & PHYSICS DEPARTMENT

## UNIVERSITY EXAMINATION FOR:

BACHELOR OF TECHNOLOGY IN APPLIED PHYSICS AND BACHELOR  
OF TECHNOLOGY IN ENVIRONMENTAL PHYSICS & RENEWABLE  
ENERGY

APS 4304: CLASSICAL MECHANICS

END OF SEMESTER EXAMINATION

**SERIES: MAY 2016**

**TIME: 2 HOURS**

**DATE: MAY 2016**

### Instructions to Candidates

You should have the following for this examination

-Answer Booklet, examination pass and student ID

This paper consists of 4 questions.

**Do not write on the question paper. Answer question ONE (compulsory) and any other two questions.**

SECTION A (30POINTS)

### QUESTION 1

(a) (i) Give the expression for angular momentum in terms of  $\mathbf{r}$  and  $\mathbf{p}$  where  $\mathbf{r}$  is the displacement and  $\mathbf{p}$  is the linear momentum of a particle moving in a circle of radius  $rl$ . [3points]

(ii) The torque of on an object is given by  $\mathbf{N} = \mathbf{r} \times \mathbf{F}$  where  $\mathbf{F}$  is the force creating the torque. Show that  $\frac{d}{dt} \mathbf{L} = \mathbf{N}$  and explain what it means when  $\mathbf{N} = 0$ . [4points]

(b) A bat of mass  $m$  perches on the outside of edge of a freely turning ceiling fan of rotational inertia  $I$  and radius  $r$ . By what ration does the angular momentum of the fan

change?

[5points]

(c) Consider a one dimensional potential,

$$U(x) = -\frac{wl^2(x^2 + l^2)}{x^4 + 8l^4}$$

(i) Sketch the potential.

[5points]

(ii) Is the motion bounded or unbounded?

[3points]

(iii) Where are the equilibrium values and are they stable or unstable?

[5points]

(d) The total energy of some particle is given by the equation

$$E = T + U. \text{ Assuming that } \mathbf{F} \cdot d\mathbf{r} = d\left(\frac{1}{2}mv^2\right) = dT, \text{ show that}$$

$$\frac{dE}{dt} = (\mathbf{F} \cdot \nabla U) \cdot \mathbf{r} + \mathbf{p} \cdot \frac{\partial U}{\partial t}$$

[5points]

## SECTION B

### QUESTION 2

(a) In the figure above, a block slides down an inclined plane without friction.

(i) Compute its acceleration

[3points]

(ii) Compute its velocity after it has moved a distance  $x_0$  down the plane from rest.

[5points]

(iii) If the coefficient of friction between the block and plane is  $\mu_s = 0.4$ , at what angle

„ will the block start sliding if it is initially at rest? [6points]

(b) Find the displacement of a particle undergoing vertical motion in a medium having a retarding force proportional to the velocity. [6points]

### QUESTION 3

(a) A system consists of a spring whose one end is fixed to an immovable wall while the other end is a mass  $m$  kg attached to it. The spring which has a spring constant  $k$  is stretched a distance  $x$  and released.

(i) Write down the equation of motion of the mass. [3points]

(ii) Solve the equation in a general form and decide which part of the equation satisfies the physical condition of the system. [7points]

(iii) What are the frequency and period of the oscillation mass? [4points]

(iv) Compute the maximum potential energy and maximum kinetic energy of the mass. [6points]

### QUESTION 4

(a) Consider a projectile motion in two dimensions. Find the equation of motion in both Cartesian and polar coordinates. [8points]

(b) (i) A particle is constrained to move on the inside surface of a smooth cone of half angle  $\alpha$ . The particle is subject to a gravitational force. Determine a set of generalized coordinates and find the constraints. [7points]

(ii) Find the Lagrange's equations of motion [5points]