

#### TECHNICAL UNIVERSITY OF MOMBASA

# FACULTY OF APPLIED AND HEALTH SCIENCE DEPARTMENT OF MATHEMATICS AND PHYSICS

# UNIVERSITY EXAMINATION FOR THE DEGREE OF BACHELOR OF SCIENCE IN MATHEMATICS AND COMPUTER SCIENCE. AMA 4326: FLUID MECHANICS II

END OF SEMESTER EXAMINATION: MAY 2016 - SERIES

**TIME:** 2 HOURS

#### **Instructions to Candidates**

You should have the following to do this examination:

-Answer Booklet, examination pass and student ID

Do not write on the question paper.

Answer question one and any other two

#### **Question one: 30 marks (Compulsory)**

i) Inversion 1 mark

ii) Enlargement 1 mark

b) Prove that  $w = W + i\mathbb{E}$  is an analytic function. 4 marks

c) Two parallel plates kept 100mm apart have laminar flow of oil between them with a maximum velocity of 1.5m/s and viscosity of oil 2.45Ns/m<sup>2</sup>.

a) Briefly describe the following standard conformal transformations:

Calculate: i) The discharge per metre width. 2 marks

ii) The shear stress at the plates. 3 marks

- d) Find a relevant stream function for a set of velocity components  $u = \frac{-cx}{v}$  and  $v = c \ln xy$  to obtain a steady incompressible flow.
  - 6 marks

e) State the Blasius theorem.

3 marks

f) What is the irrotational velocity field associated with the potential

 $W = 3x^2 - 3x + 3y^2 + 16t^2 + 12zt$ . Does the flow field satisfy the incompressible continuity equation? 5 marks

g) Prove that the transformation  $w = \frac{1}{7}$  maps the circle  $x^2 + y^2 + 2gx + 2fy + c = 0$  in the Z plane onto a circle in the w plane and maps circles in the Z plane through the origin onto a straight line in the w-plane. 5 marks

# **Question TWO (20 marks)**

- a) Fluid is in laminar motion between two parallel plates under the action of motion on one of the plates and also under the presence of a pressure gradient in such a way that the net forward discharge across any section is zero:
- 7 marks i) Find out the point where minimum velocity occurs and its magnitude.
- ii) Draw the velocity distribution profile (sketch graph) across a section of the parallel plates.

2 marks

- b) The velocity components in a fluid flow are given by U = 2xy and  $V = a^2 + x^2 y^2$ 
  - i) Show that the flow is possible.

2 marks

ii) Derive the relative stream function.

4 marks

c) If streamlines are represented by  $\mathbb{E} = x^2 + y^2$  determine the velocity and its direction at (3, 4)

5 marks

## **Question THREE (20 marks)**

a) Discuss the flow pattern due to a line source at the origin of a complex potential function.

4 marks

- b) In a pipe of 300mm diameter the maximum velocity of flow is found to be 2m/s, if the flow in the circular pipe is laminar. Find:
  - i) The average velocity and the radius at which it occurs.

5 marks

ii) The velocity at 50mm from the wall of the pipe.

- 2 marks
- c) Consider a conformal mapping  $w = \sqrt{z}$ , show that the curve |z 1| = 1 transforms to
  - ...<sup>2</sup> =  $2\cos 2w$  where  $w = ...e^{iw}$  in the w plane.

6 marks

d) Determine a relevant stream function to a set of velocity components of steady incompressible flow if u=2cx and v=-2cy.

3 marks

#### **Question FOUR (20 marks)**

- a) Define the following terms as used in fluid mechanics:
  - i) Incompressible flow.

1 mark

ii) Equipotential line.

1 mark

- b) Discuss the flow due to a uniform line doublet at point O of strength ~ per unit length if its axis is along the x- axis.7 marks
- c) A lubricating oil of viscosity 1 poise and specific gravity 0.9 is pumped through a 30mm diameter pipe, if the pressure drop per metre length of pipe is 20KN/m<sup>2</sup>. Determine
  - i) The mass flow rate in kg/min.

4 marks

ii) Shear stress at the pipe wall.

2 marks

iii) The Reynolds number for the flow.

2 marks

d) Show whether the function  $\mathbb{E} = A(x^2 - y^2)$  represents a possible irrotational flow. 3 marks

# Question FIVE (20 marks)

- a) The velocity distribution in a pipe is given by  $\frac{U}{U \max} = 1 \left(\frac{r}{R}\right)^n$  where  $U_{\max}$  is the maximum velocity at the centre of a pipe, U is the velocity at a distance r from the centre and R is the pipe radius. Obtain an expression for mean velocity in terms of  $U_{\max}$  and n. 5 marks
- b) The flow field of a fluid is given by  $V = xyi + 2yzj (yz + z^2)k$ :
  - i) Show that it represents a possible 3 dimensional steady incompressible continuous flow.

2 marks

ii) Is this flow rotational or irrotational.

2 marks

- iii) If irrotational determine at point A (2, 4, 6) the value of angular velocity and vorticity. 4 marks
- b) If there is a line source of strength m at a point Z and a line source of equal strength at the mirror image of  $z_1$  at the line x=0. Prove that there is no fluid motion across the mirror x=0.

  7 marks

### THE END