



THE MOMBASA POLYTECHNIC UNIVERSITY COLLEGE

Faculty of Engineering & Technology

DEPARTMENT OF CIVIL AND BUILDING ENGINEERING

DIPLOMA IN CIVIL AND CONSTRUCTION &

DIPLOMA IN BUILDING AND CIVIL (08)

END OF FINAL EXAMINATIONS

APRIL/MAY 2010 SERIES

AH 2203 - ORDINARY DIFFERENTIAL EQUATIONS (ODE)

TIME: 2 HOURS

Instructions to Candidates

This paper consists of **TWO** Section i.e. Section A which is **COMPULSORY**, and Section **B**. In Section **B**, choose any **TWO** Questions and maximum marks for each question is shown.

SECTION A - (COMPULSORY)

Question ONE

- (a). (i). Using Laplace transform, solve the equation.
 $(D^2 + 2D + 2)y = e^{-t}$
Assume zero initial conditions.

(10 Marks)

(ii). Solve $\frac{2d^2y}{dx^2} - 5\frac{dy}{dx} - 3y = 4\sin 2x$

(20 Marks)

SECTION B - (CHOOSE ANY TWO)

Question TWO

- (a). Using Laplace transform, solve $(D^2 - 3D + 2)x = 0$, given that when $t=0$, $x=4$
and $\frac{dx}{dt} = 3$.

(10 Marks)

- (b). Determine Laplace transform of the following:

(i). $L\{\cos at\}$

(ii). $L\{t\}$

(iii). $L\{e^{-t} \cos 3t\}$

(iv). $L\left\{\frac{5}{3}e^{-2t} \sin 3t\right\}$

(10 Marks)

Questions THREE

(a). Solve, $\frac{d^2y}{dx^2} - 2\frac{dy}{dx} + y = 3e^x$

(15 Marks)

- (b). Determine solution of the following Laguerres differential polynomial,

$x\frac{d^2y}{dx^2} + (1-x)\frac{dy}{dx} + ny = 0$

(5 Marks)

Question FOUR

(a). Solve $\frac{d^2y}{dx^2} + 4\frac{dy}{dx} = 6$

(8 Marks)

(b). Using Laplace transform, solve the following simultaneous differential equations.

$$(D^2 + 4)x - 2Dy = 2$$

$$Dx + CD^2 + 4jy = 0$$

Given that $x = 1, y = Dx = Dy = 0, \text{ at } t = 0.$

(12 Marks)

Question FIVE

Find the solution following Bessel's equation;

$$x^2 \frac{d^2y}{dx^2} + x \frac{dy}{dx} + (x^2 - n^2)y = 0$$

(20 Marks)