



# THE MOMBASA POLYTECHNIC UNIVERSITY COLLEGE

*Faculty of Engineering and Technology*

DEPARTMENT OF ELECTRICAL & ELECTRONIC ENGINEERING

## DIPLOMA IN TECHNOLOGY

**EEC 2203**

### CONTROL SYSTEMS I

END OF SEMESTER EXAMINATION

**SERIES:** FEBRUARY 2011 SERIES

**TIME:** 2 HOURS

#### **Instructions to Candidates:**

1. You are required to have the following for this examination;
  - Answer booklet
  - A non-programmable calculator
  - La Place transform tables
2. Answer Question **ONE (COMPULSORY)** and any other **TWO** Questions.
3. Maximum marks for each question are shown.

(COMPULSORY)

**Question ONE**

- a) i) With the aid of a canonical form block diagram of a closed loop system derive closed loop transfer function

$$\frac{C_{(s)}}{R_{(s)}} = \frac{G_{(s)}}{1 + G_{(s)}H_{(s)}}$$

- ii) Define the following control terms

- I) System
- II) Controlled variable
- III) Reference variable
- IV) Plant
- V) Error signal

- iii) State FOUR features that feedback effects to a system. (15marks)

- b) Reduce the block diagram in figure 1 to open loop form hence find the relationship

$$\frac{R_{(s)}}{C_{(s)}} \quad (5 \text{ marks})$$

**Fig 1**

- c) Reduce the signal flow graph in fig 2 to get the ratio of output to input.

$$\frac{X_s}{X_1} \quad (6 \text{ marks})$$

**Fig 2**

- d) Obtain the transfer function of the fig 3 below (4 marks)

**Fig 3**

(ANSWER ANY OTHER TWO QUESTIONS)

**Question TWO**

- a) Construct the signal flow graph of the following simultaneous equations making  $y_4$  as the output node hence determine the transfer function using Masous gain formula. (15marks)

$$y_2 = t_{21} y_1 + t_{23} y_3$$

$$y_3 = t_{31} y_1 + t_{32} y_2 + t_{33} y_3$$

$$y_4 = t_{42} y_2 + t_{43} y_3$$

- b) Define the following terms as used in signal flow graphs (5 marks)
- i) Feedback loop
  - ii) Self loop
  - iii) Input node
  - iv) Output node
  - v) Path

**Question THREE**

- a) Define with the aid of sketches the following input signals used for testing control systems. Give their mathematical representation.

- i) Step
- ii) Impulse
- iii) Ramp
- iv) Parabolic

- b) For the system shown in fig 4 below, find 'a' such that the damping ratio is 0.5. Determine the:

- i) Rise time
- ii) Peak time
- iii) Maximum overshoot
- iv) Settling time

In the unit step response input.

(10marks)

**Fig 4**

**Question FOUR**

- a) Simplify the block diagram in fig 5 below hence determine the outputs  $G_{(s)}$  (16marks)

**Fig 5**

- b) Simplify the block diagram in figure 6 below and obtain closed loop transfer function.

$$\frac{C_{(s)}}{R_{(s)}} \quad (4 \text{ marks})$$

**Fig 6**

### **Question FIVE**

- a) For the spring mass damper system shown in fig 7 below shows that when subjected to a forcing function  $F(t)$ , it shifts from rest position  $X_0$  to final displacement  $X_1$  by the value:

$$F(t) = mx_1 + Cx_1 + kx_1 \quad (6 \text{ marks})$$

**Fig 7**

Where

- $X_0$  = initial position  
 $X_1$  = position after displacement  
 $M$  = mass  
 $K$  = spring  
 $C$  = damper

- b) For a system described by

$$\frac{d^2 y}{dt^2} + 5 \frac{dy}{dt} + 6y = 6$$

With initial conditions

$$y'(0) = 2; \quad y(0) = 2. \text{ Obtain } y(t).$$

Using Laplace transforms obtain value of  $y(t)$

(8 marks)

- c) For the circuit shown in fig 8 below, determine the relationship.

(6 marks)

$$\frac{E_{o(s)}}{E_{i(s)}}$$

**Fig 8**