



TECHNICAL UNIVERSITY OF MOMBASA

Faculty of Applied & Health Sciences

DEPARTMENT OF MATHEMATICS & PHYSICS

UNIVERSITY EXAMINATION FOR THE BACHELOR OF SCIENCE IN
MECHANICAL ENGINEERING

EMG 2414: NUMERICAL METHODS FOR ENGINEERS

SPECIAL/SUPPLEMENTARY EXAMINATION

SERIES: MARCH 2014

TIME: 2 HOURS

Instructions to Candidates:

You should have the following for this examination

- *Answer Booklet*

This paper consist of **FIVE** questions in **TWO** sections **A & B**

Answer question **ONE (COMPULSORY)** and any other **TWO** questions

Maximum marks for each part of a question are as shown

This paper consists of **THREE** printed pages

SECTION A (COMPULSORY)

Question One

$$A = \begin{pmatrix} 8 & 3 \\ 2 & 7 \end{pmatrix}$$

a) Find the eigen values and eigen vectors of **(5 marks)**

$$L = (D^2 + 3D + 2) \quad f_1(t) = t^3 \quad f_2(t) = \cos t \quad L(3f_1(t) + 4f_2(t))$$

b) Given that and , evaluate **(5 marks)**

$$A = \begin{pmatrix} 3-2i & 1+i \\ 2-i & -2+3i \end{pmatrix}$$

c) If find A^* (3 marks)

$$\int_1^3 \frac{2}{\sqrt{x}} dx$$

d) Use trapezoidal rule with 8 intervals to evaluate: correct to 3 decimal places (5 marks)

e) Find the approximate values of y at $t = 0.1, 0.2, 0.3$ and 0.4 using Euler's method with a step size of $h = 0.1$ given that $y' + 2y = 2 - e^{-4t}$ and $y(0) = 1$ (7 marks)

$$y' = 3x + 2y$$

f) Apply Taylor series to solve the differential equation at $x = 0.2$ given that $y(0) = 1$ (5 marks)

SECTION B (Answer any TWO questions from this section)

Question Two

$$\int_0^{\pi/3} \sqrt{1 - \frac{1}{3}} \sin^2 \theta d\theta$$

a) Evaluate correct to 3 d.p using Simpsons rule with 6 intervals. (7 marks)

b) Solve the system using the matrix method:

$$\frac{dx}{dt} = 6x + 5y$$

$$\frac{dy}{dt} = x + 2y$$

(7 marks)

c) Use row reduction to find the inverse of the following matrix:

$$M = \begin{pmatrix} 3 & 0 & 2 \\ 2 & 0 & -2 \\ 0 & 1 & 1 \end{pmatrix}$$

(6 marks)

Question Three

$$r = u + at$$

a) The velocity of a car accelerating at uniform acceleration a between two points is given by where u is its velocity when passing the first point and t is the time taken to pass between the two points. If $v = 21\text{m/s}$ when $t = 3.5\text{s}$ and $r = 33\text{ m/s}$ when $t = 6\text{s}$ use determinants to find the values of u and a correct to 4 significant figures. (5 marks)

b) Use Cramer's Rule to solve the system of linear equations (7 marks)

$$\begin{aligned} 3x + y + z &= 3 \\ 2x + 2y + 5z &= -1 \\ x - 3y - 4z &= 2 \end{aligned}$$

- c) Apply the modified Euler's method to determine the approximate values of y given that $y' = x + y$, $y(0) = 1$ $0 \leq x \leq 0.04$ and with $h = 0.02$ **(8 marks)**

Question Four

- a) Use the fourth order Runge – Kutta method to solve $y' = y^2 + 1$: $y(0) = 0$ on the interval $(0, 0.3)$ with $h = 0.1$. **(9 marks)**

- b) In two closed loops of an electrical circuits the current flowing are given by the simultaneous equations:

$$\begin{aligned} I_1 + 2I_2 + 4 &= 0 \\ 5I_1 + 3I_2 - 1 &= 0 \end{aligned}$$

Use to solve for I_1 and I_2 Kirchoffs method **(6 marks)**

- c) Convert each of the following into normal system.

(i) $\frac{d^2x}{dt^2} - \frac{5dx}{dt} + x = e^{4t}$ **(2 marks)**

(ii) $\frac{d^3x}{dt^3} + 2\frac{d^2x}{dt^2} - \frac{7dx}{dt} = 2t^2 + 1$ **(3 marks)**

Question Five

- a) Use Romberg method to compute:

$$\int_0^1 \frac{dx}{1+x}$$

correct to 4 d.p
 $I\left(\frac{h}{2}\right) = 0.69$ $I\left(\frac{h}{4}\right) = 0.6941$

$h = 0.5$, $I(a) = 0.7084$, I and **(6 marks)**

- b) Applying Gauss and quadrature formula for the interval $(-1, 1)$ to compute the integral:

$$I = \int_5^{12} \frac{dx}{x}$$

choosing $n = 3$

(8 marks)

$$\int_0^{\pi/2} \frac{1}{1 + \sin x} dx$$

c) Use the trapezium rule to evaluate

using 6 intervals

(6 marks)