



THE MOMBASA POLYTECHNIC UNIVERSITY COLLEGE

(A Constituent College of JKUAT)
Faculty of Applied & Health Sciences

DEPARTMENT OF MATHEMATICS & PHYSICS

UNIVERSITY EXAMINATION FOR BACHELOR OF SCIENCE IN
ELECTRICAL/ELECTRONICS ENGINEERING

SMA 2471: NUMERICAL ANALYSIS

SPECIAL/SUPPLEMENTARY EXAMINATION

SERIES: MAY/JUNE 2012

TIME: 2 HOURS

Instructions to Candidates:

You should have the following for this examination

- Answer Booklet

This paper consists of **FIVE** questions

Answer question **ONE (COMPULSORY)** and any other **TWO** questions

Maximum marks for each part of a question are clearly shown

This paper consists of **THREE** printed pages

Question 1 (Compulsory - 30 Marks)

$$f(x) = \sin x, x = 0^\circ(10)50^\circ$$

- a) By tabulating and using Newton's forward difference interpolation formula of degree four, estimate $\sin 7^\circ$ to four decimal places. (6 marks)

$$\frac{dy}{dx} = -y \text{ for } x = 0.6 \text{ and } h = 0.2$$

- b) Use Euler's modified method to solve with boundary conditions when $y = 1$ when $x = 0$ (7 marks)

$$\int_0^6 \sqrt{1+x^4} dx$$

- c) Estimate using Simpson's Rule with $n = 6$ (6 marks)

- d) Apply Newton-Raphson method to find the real roots of $x^2 - 5x + 2 = 0$ correct to 4 decimal places (7 marks)
- e) Determine the maximum step size to be used in the tabulation of $f(x) = (1 + 2x)^6$ on $[0,1]$ so that the truncation error for Linear interpolation is correct to 5 decimal places. (4 marks)

Question 2 (20 Marks)

- a) Using Picard's process of successive approximations, obtain a solution to the fifth approximation

$$\frac{dy}{dx} = y + x, y(0) = 1, h = 0.1$$

of the equation (6 marks)

$$\int_0^1 \frac{dx}{1+x}$$

- b) Use Romberg method to computer $\int_0^1 \frac{dx}{1+x}$ correct to 4 decimal places given that for $h = 0.5, I(h) = 0.7084, I\left(\frac{h}{2}\right) = 0.6970$ and $I\left(\frac{h}{4}\right) = 0.6941$ (4 marks)
- c) Fill in the table for the missing values of $f(x)$ correct to 3 decimal places

x	$\frac{\pi}{6}$	$\frac{\pi}{9}$	$\frac{5\pi}{18}$	$\frac{\pi}{3}$	$\frac{7\pi}{18}$
$F(x) = \sin^2 \frac{1}{2}x$		2			

Use Simpson's Rule to find the area under the curve represented by $f(x)$. Determine the truncation effort expected in the calculated value (10 marks)

Question 3 (20 Marks)

$$\frac{dy}{dx} = x^3 + y^2, y(0) = 0$$

- a) For the equation use $h = 0.2$ to find $y(0.2), y(0.4)$ and $y(0.6)$ using the Runge – Kutta fourth order method. (10 marks)

$$I = \int_5^{12} \frac{dx}{x}$$

- b) Apply the Gauss' quadrature formula to compute the integral $\int_5^{12} \frac{dx}{x}$ choosing $n = 3$ in the interval $(-1,1)$ (7 marks)
- c) Using $\sin 0.1=0.09983$ and $\sin 0.2=0.198867$ find an approximate value of $\sin 0.15$ by Lagrange interpolation. (3 marks)

Question 4 (20 Marks)

a) By means of Newton's divided difference formula find the value of $f(15)$ from the following table

x	4	5	7	10	11	13
f(x)	48	100	294	900	1210	2028

(6 marks)
 $\frac{dy}{dx} = x + y$

b) Using the Taylor's series method to the 4th order derivative, estimate $y(0.5)$ given that $y(0) = 1$

with taking $h = 0.1$ to 4 decimal places (6 marks)

c) Approximate $y(0.4)$ using the Adams-Bashforth predictor corrector method for the equation

$$\frac{dy}{dx} = -2xy$$

given that:

x	0	0.1	0.2	0.3	0.4
y	1.00	0.990	0.9608	0.9139	0.8522

(7 marks)

Question 5 (20 Marks)

$$\int_0^1 \frac{dx}{1+x}$$

a) Use Trapezoidal rule to evaluate (6 marks)

b) Apply Newton's divided difference to find the value of $f(8)$ if $f(1) = 3, f(3) = 31, f(6) = 223, f(10) = 1011, f(11) = 1343$

(8 marks)

c) Find the function U_x in powers of $x-1$ given that $U_0 = 8, U_1 = 11, U_4 = 68, U_5 = 123$

(6 marks)