



TECHNICAL UNIVERSITY OF MOMBASA
Faculty of Applied & Health
Sciences

DEPARTMENT OF MATHEMATICS & PHYSICS
DIPLOMA IN MECHANICAL ENGINEERING (DMEN 4)

AMA 2251: ENGINEERING MATHEMATICS IV

END OF SEMESTER EXAMINATION
SERIES: DECEMBER 2014
TIME ALLOWED: 2 HOURS

Instructions to Candidates:

You should have the following for this examination

- *Answer Booklet*

This paper consist of **FIVE** questions

Answer question **ONE (COMPULSORY)** and any other **TWO** questions

Maximum marks for each part of a question are as shown

This paper consists of **THREE** printed pages

Question One (Compulsory)

$$f(t) = e^{2t}t^2 + e^{-t} \cos t$$

a) (i) Determine the Laplace transform of **(4 marks)**

$$F(s) = \frac{s+3}{s^2-4}$$

(ii) Determine the inverse Laplace transform of **(8 marks)**

$$F(t) = e^{4t}$$

(iii) Obtain from first principles the Laplace transform of **(4 marks)**

b) (i) Use Maclaurin's series to obtain the first three terms of the power series for

$$\frac{d^2y}{dt^2} + 4\frac{dy}{dt} + 5y = 6\sin t$$

$$f(x) = \cos 2x$$

use Maclaurin's theorem to obtain the power series for

(5 marks)

$$f(x) = x^4 + 2$$

(ii) Use Taylor's series to express the function as a power series of $x + 1$

(8 marks)

c) Determine the Newton-Gregory forward difference interpolating polynomial for the data below. Hence evaluate $f(25)$ **(6 marks)**

x	0	1	2	3	4
f(x)	1	7	23	55	109

Question Two

$$F(t) = \sin^2 t$$

a) Determine the Laplace transform **(3 marks)**

$$F(s) = \frac{s+2}{s^2+25+2}$$

b) Determine the inverse Laplace transform of **(5 marks)**

c) Use Laplace transforms to solve the differential equation.

$$2\frac{dy}{dt} - y = \sin t$$

given at $t = 0, y = 1$

(12 marks)

Question Three

$$f(x) = (e^x + 1)\ln(1+x)$$

a) Use Maclaurin's series to obtain the first three terms of the power series for

(10 marks)

$$\tan(x+h)$$

b) Use Taylor's series to obtain the power series for up to the term in h^2 . Hence obtain the

$$\tan\left(\frac{\pi}{4} + h\right)$$

$$\tan 46^\circ$$

power series for and use it to determine correct to four decimal places.

(10 marks)

Question Four

$$x_0 = -1.3$$

- a) Apply the Newton-Raphson method taking $x^3 - 6x^2 + 12 = 0$ to determine correct to 4 significant figures the root of the equation **(6 marks)**

- b) The data in the table below defines a function:

x	1	2	3	4	5	6
f(x)	4	14	40	88	164	274

$$f(2.5)$$

- (i) Use the Newton-Gregory forward difference formula to evaluate
 (ii) Use the Newton-Gregory backward difference formula to evaluate $f(5.8)$

(14 marks)

Question Five

- a) Solve using the Laplace transforms of the differential equation:

$$\frac{dx}{dt} + 2x = 10e^{3t}$$

give at $t = 0, x = 16$

(10 marks)

$$f(x) = \cos(x + h)$$

- b) Use Taylor's series to obtain the power series for $\cos\left(\frac{\pi}{3} + h\right)$ up to the term in h^4 . Hence obtain the power series for $\cos 62^\circ$ and use it to determine the value of $\cos 62^\circ$ correct to 4 decimal places. **(10 marks)**