



TECHNICAL UNIVERSITY OF MOMBASA

Faculty of Applied & Health Sciences

DEPARTMENT OF MATHEMATICS & PHYSICS

UNIVERSITY EXAMINATION FOR DEGREE OF:

BACHELOR OF TECHNOLOGY IN RENEWABLE ENERGY
BACHELOR OF TECHNOLOGY IN APPLIED PHYSICS
(BTRE 14G/BTAP 14G)

APS 4105: ELECTRICITY & MAGNETISM I

SPECIAL/SUPPLEMENTARY EXAMINATION

SERIES: JUNE/JULY 2015

TIME ALLOWED: 2 HOURS

Instructions to Candidates:

You should have the following for this examination

- *Mathematical tables*
- *Scientific Calculator*

This paper consist of **FOUR** questions

Answer question **ONE (COMPULSORY)** and any other **TWO** questions

Maximum marks for each part of a question are as shown

This paper consists of **FOUR** printed pages

$$\epsilon_0 = 8.85 \times 10^{-12} \text{ Fm}^{-1} \quad K = 1/4\pi\epsilon_0 = 9 \times 10^9 \text{ Nm}^2\text{C}^{-2}$$

Permittivity of free space

$$\mu_0 = 4\pi \times 10^{-7} \text{ Hm}^{-1}$$

Permeability of free space

$$m_e = 9.11 \times 10^{-31} \text{ kg}$$

Electron mass,

$$M_p = 1.67 \times 10^{-27} \text{ kg}$$

Proton mass

$$\mu_0 = 1.6 \times 10^{-19}$$

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Question One (Compulsory)

- a) (i) State Coulomb's law for the electrostatic force between two joint charges **(1 marks)**
- (ii) Three identical point charges, each $1\mu\text{C}$, are placed at the vertices of an equilateral triangle 10cm apart. Calculate the force on each charge **(4 marks)**
- b) An isolated positive point charge $Q = 2\mu\text{C}$:
- (i) Determine the electric field \vec{E} and also the potential, V , due to this charge at point P which is 10cm away from the charge. **(4 marks)**
- (ii) Determine the work done in bringing an identical charge from infinity to point P **(3 marks)**
- (iii) Sketch the electric field lines and equipotential lines associated with this isolated point charge **(3 marks)**
- c) A point charge $Q_1 = +27\mu\text{C}$ is placed at coordinate (0, 0) while another charge $Q_2 = +3\mu\text{C}$ is at (1, 0). At what point (other than infinity) would the net force on a third point charge be zero? **(3 marks)**
- d) A parallel plate capacitor has plates with dimensions 3cm by 4cm separated by 2mm. The plates are connected across a 60V battery.
- (i) Determine the capacitance and charge on each plate **(3 marks)**
- (ii) Determine the energy stored **(3 marks)**
- (iii) A dielectric material of relative dielectric constant 6 is now inserted and plates of the capacitor. Calculate the new charge stored **(3 marks)**
- (iv) Compute the electric force between the plates when the dielectric is in plate **(3 marks)**

Question Two

- a) (i) State Gauss's Law for electrostatics **(1 mark)**
- (ii) A point charge q is at the centre of a spherical metal shell of radius R that has a net charge $-Q$. Determine the electric field and potential at a distance r outside the shell **(4 marks)**
- b) A non conducting disk of radius a has a uniform surface charge density ρcm^{-2} . Determine the electric field strength at a distance y from the centre along the central axis **(5 marks)**
- c) An electron enters the region between two horizontal charged plates with an initial horizontal velocity of $u = 2 \times 10^6\text{ms}^{-1}$ midway between the two plates. The plates are 4cm long and 1.6cm apart, see figure 1 below. The electric field within the plates is 450Vm^{-1} :
- (i) Determine the vertical displacement from the initial horizontal position that the electron undergoes within the plates **(5 marks)**
- (ii) Determine the magnetic field strength that can be introduced within the electric field so that the electron passes through the plates underdeflected. Show the orientation of the magnetic field. **(5 marks)**

Question Three

- a) The radius of a copper wire is 1.63mm. A potential difference (p.d) of 60V is applied across a 20m length of this wire resistivity of copper = $1.7 \times 10^{-8} \Omega m$. Find:
- (i) the current (3 marks)
 - (ii) the electric field (2 marks)
- b) Derive an expression for the current density, J, for a current carrying wire of cross-sectional area, A. Explain any symbols used. (3 marks)
- c) In the circuit of figure 2, the cell \mathcal{E}_1 has an emf of 15V and internal resistance of 2Ω ; and the cell \mathcal{E}_2 has emf of 4V and internal resistance of 1Ω ; and the cell \mathcal{E}_3 has emf of 4V and internal resistance of 1Ω . In the circuit $R_1 = 4\Omega$, $R_2 = 3\Omega$ and $R_3 = 2\Omega$. Determine the current i_1 , i_2 , and i_3 (7 marks)
- d) Two capacitors $C_1 = 0.1\mu F$ and $C_2 = 0.25\mu F$ are connected in series to a 12V battery.
- (i) Determine the charge on each capacitor (2 marks)
 - (ii) Calculate the potential difference across each capacitor (3 marks)

Question Four

- a) Two long, straight parallel wires are 3cm apart. They carry currents $I_1 = 3A$ and $I_2 = 5A$ in opposite directions, as shown in figure 3. I_1 is out of the paper while I_2 is into the paper.
- (i) Draw the magnetic field lines associated with these wires (2 marks)
 - (ii) Indicate the force experienced by the wires and compute the force per unit length on either wire. (3 marks)
 - (iii) Calculate the magnetic field strength at point P (3 marks)
- b) An electron with kinetic energy of $10^3 eV$ moves perpendicular to the lines of a uniform magnetic field $\vec{B} = 10^{-3} T$
- (i) If \vec{B} is into the paper, sketch the path of the electron (1 marks)
 - (ii) Determine the period and; (3 marks)
 - (iii) Compute the radius of the electron orbit in the field (4 marks)
- c) An electron has a velocity of $V = 106J ms^{-1}$ in the field $\vec{B} = 0.052 \hat{j} T$ what is the force on the electron (4 marks)